

# Properties of Embedded Clusters

## Models versus Observations

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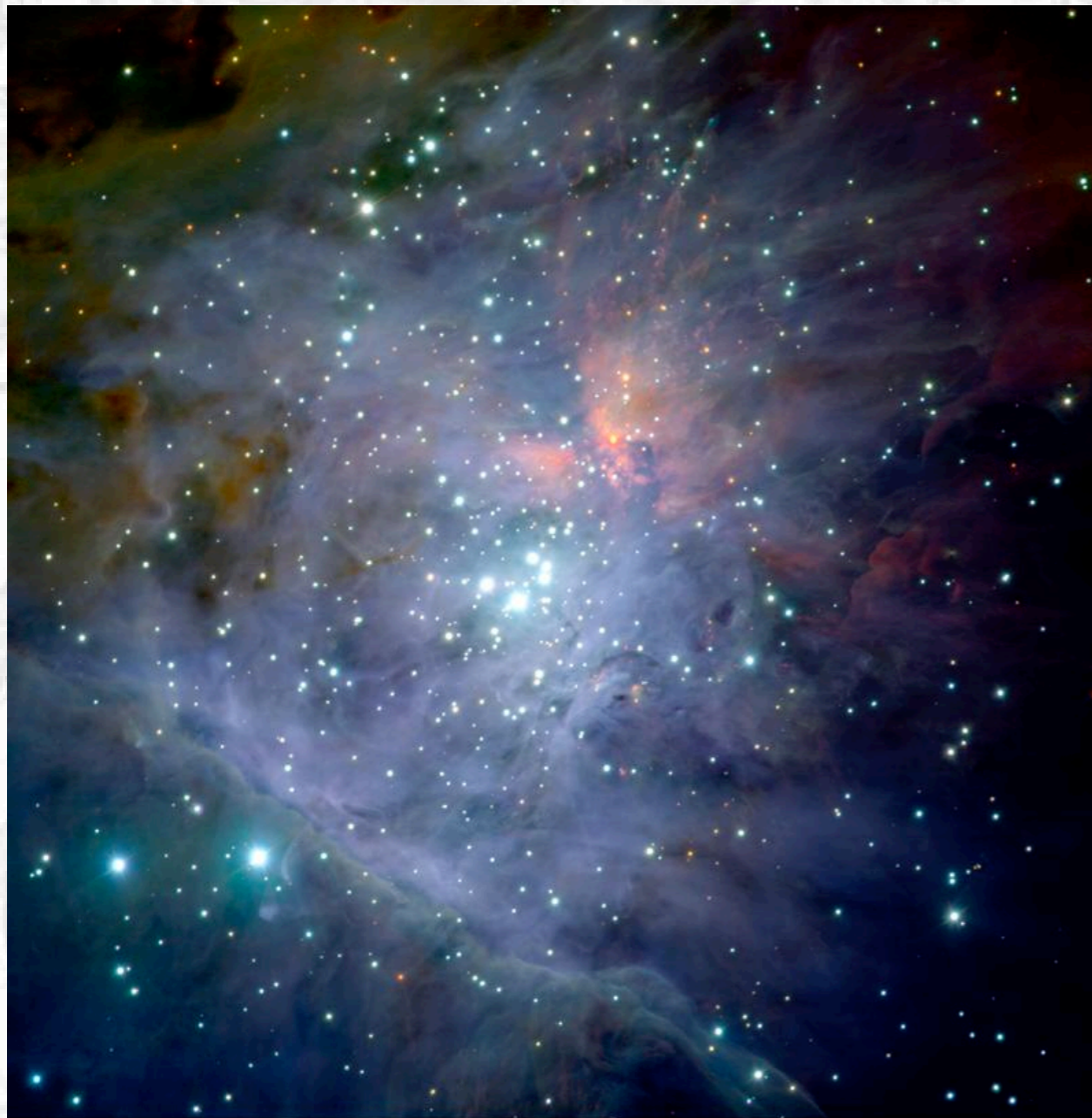
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Harvard-Smithsonian Center for Astrophysics  
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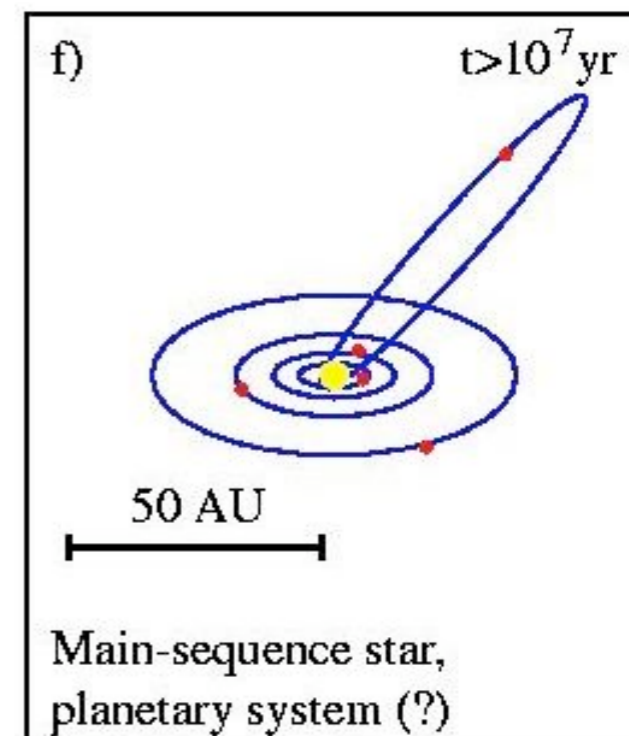
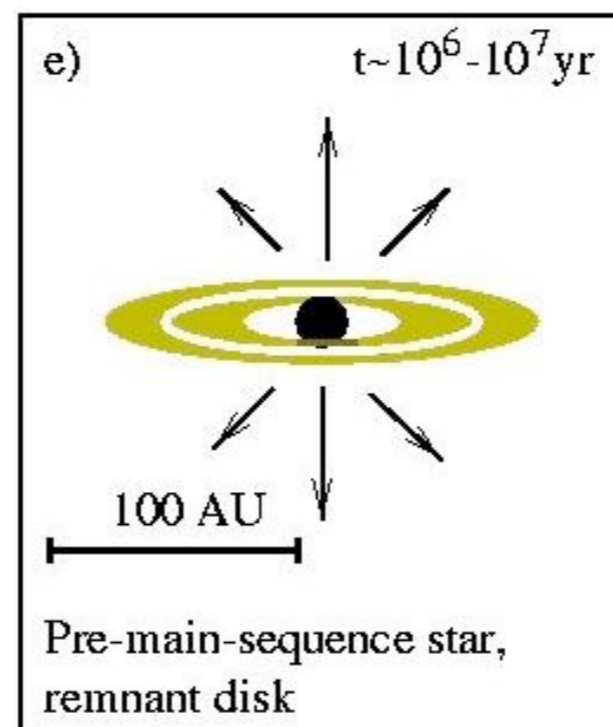
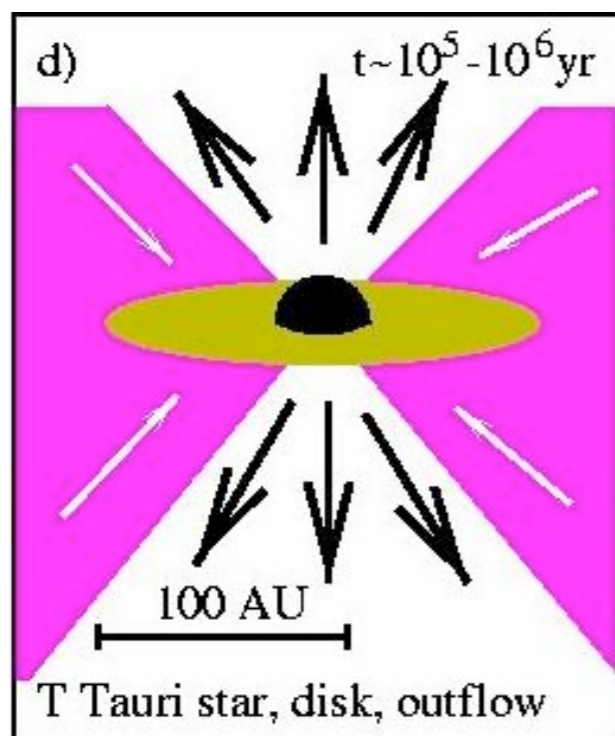
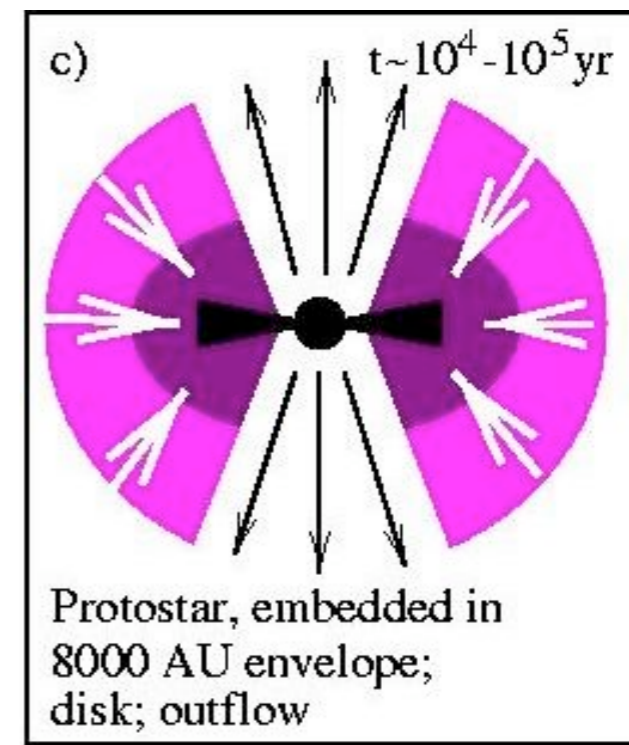
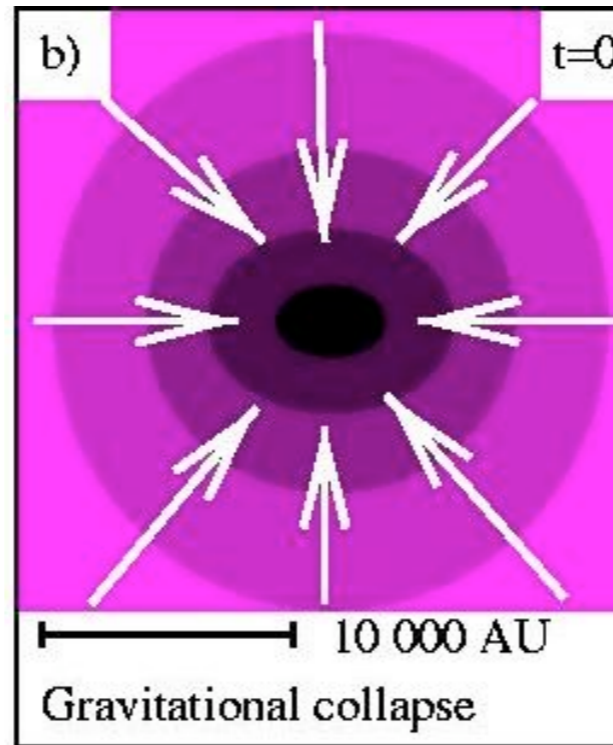
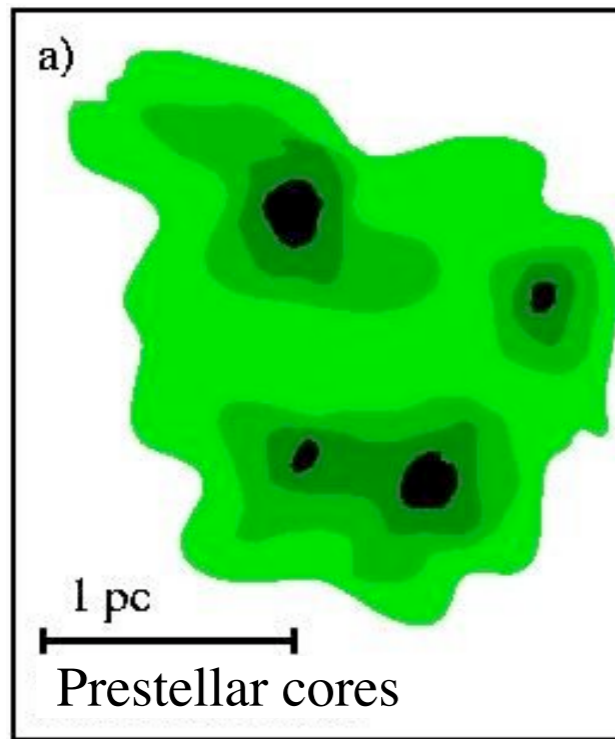
# Stars form...



M. McCaughrean, ESO

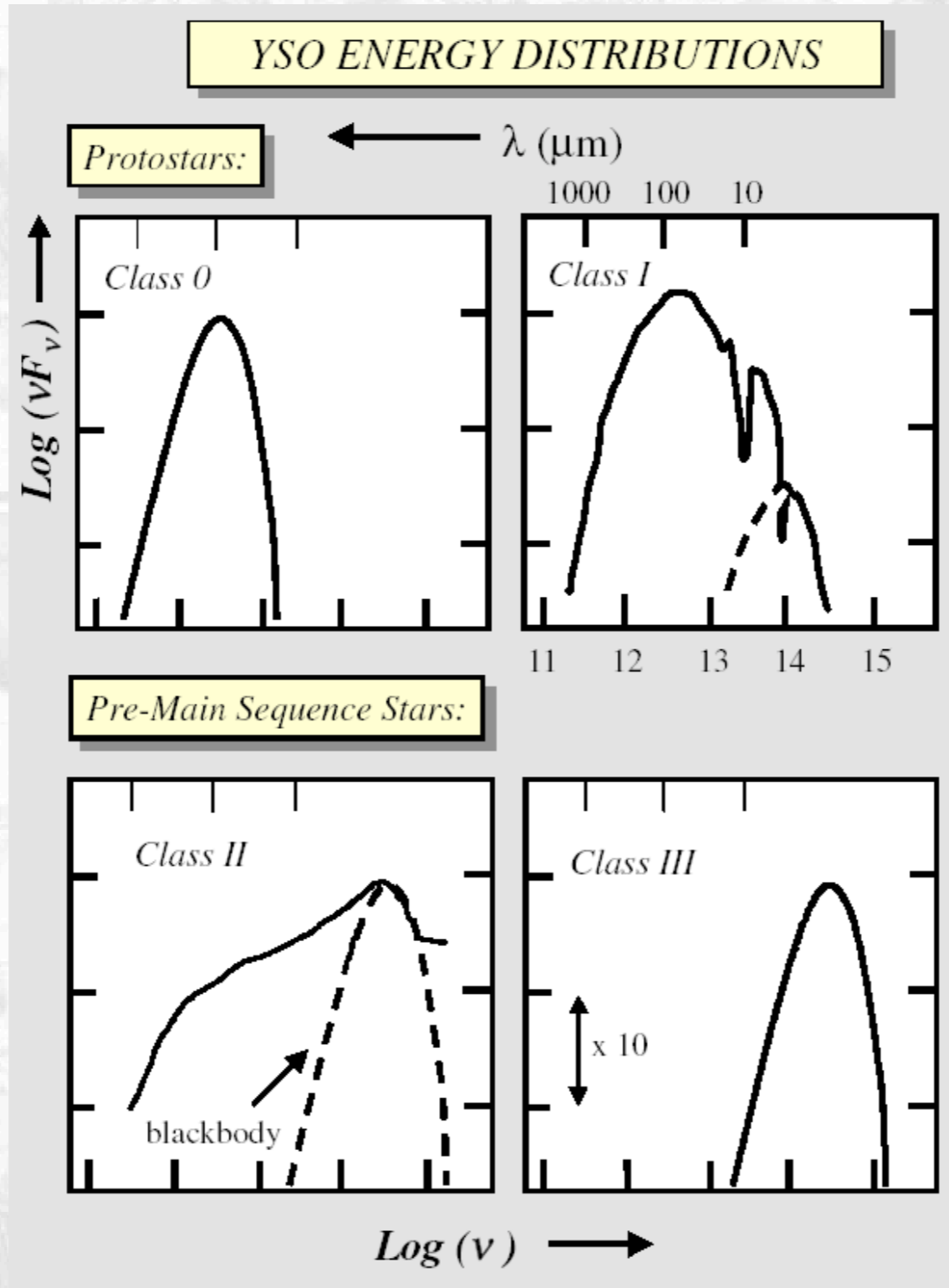
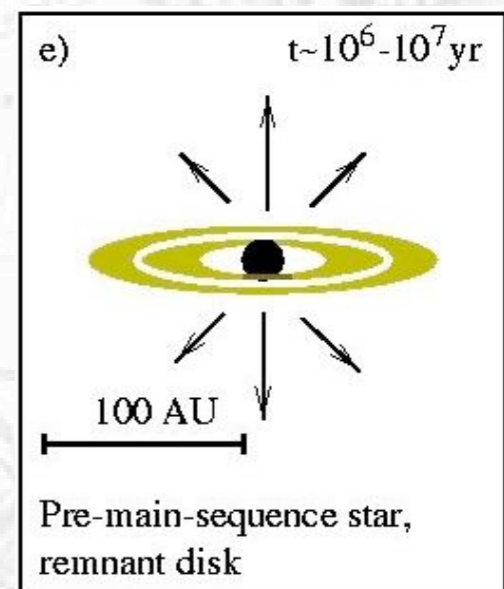
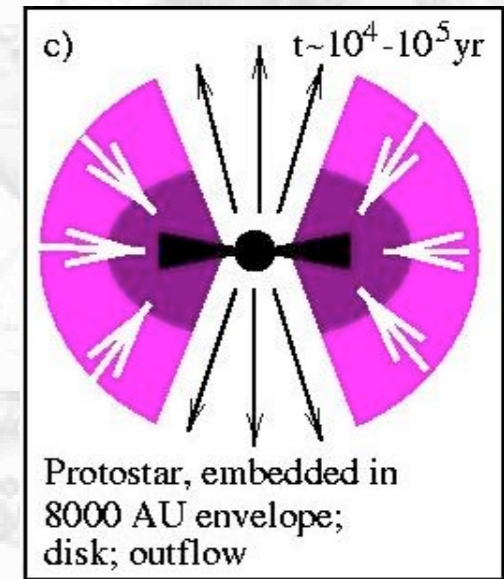
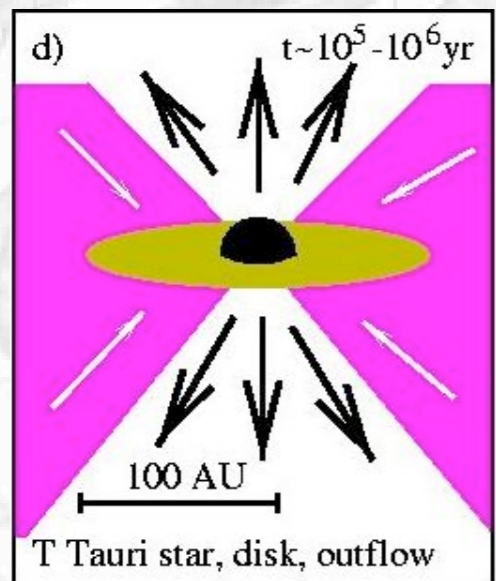
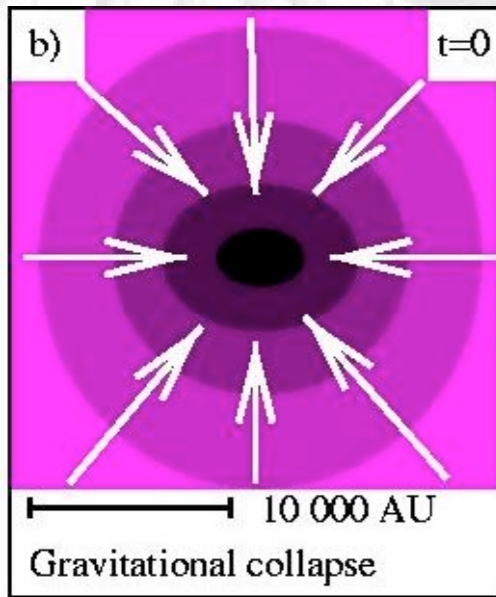
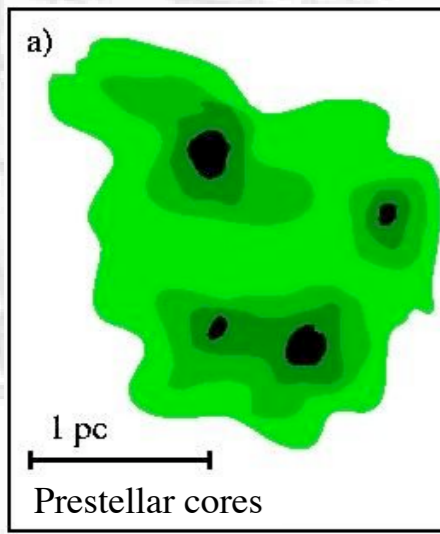
- in the dense cores of molecular clouds
- in clusters
- continuously
- with an efficiency  $\lesssim 30\%$

# From Clouds to Stars



(Hogerheijde 1998, after Shu et al. 1987)

# YSO Classification



(Hogerheijde 1998, after Shu et al. 1987; Lada 2001)

# “Standard Model” of SF

“Standard model” of star formation (Shu 1977): stars form by inside-out collapse of a **singular isothermal sphere** (SIS), initially in quasistatic equilibrium, supported against gravity by magnetic and thermal pressure evolution only due to **ambipolar diffusion** processes

## problems:

- only applicable to isolated stars
- observed magnetic fields probably not strong enough
- long timescale
- constant mass accretion rates

**→ Star formation controlled by interplay between gravity and supersonic turbulence**

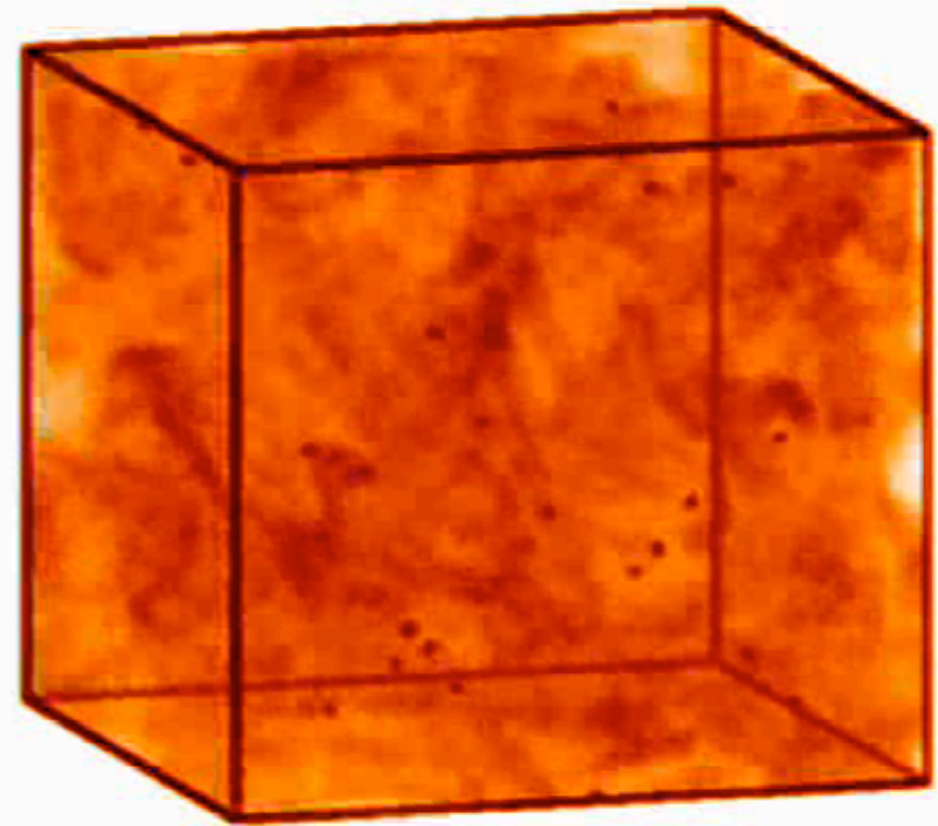
# Supersonic Turbulence

- observed **ubiquitously** within the Galaxy
- Mach numbers  $\mathcal{M} \approx 10$  ( $\mathcal{M} = v/c_s$ )
- **counterbalances gravity** on global scales
- produces strong density fluctuations → **local collapse**
- hierarchical and complex (clumpy) density and velocity structure
- moderates the star formation process (**Mac Low & Klessen 2004**)

**Turbulence plays a dual rôle!**

# Numerical Simulations

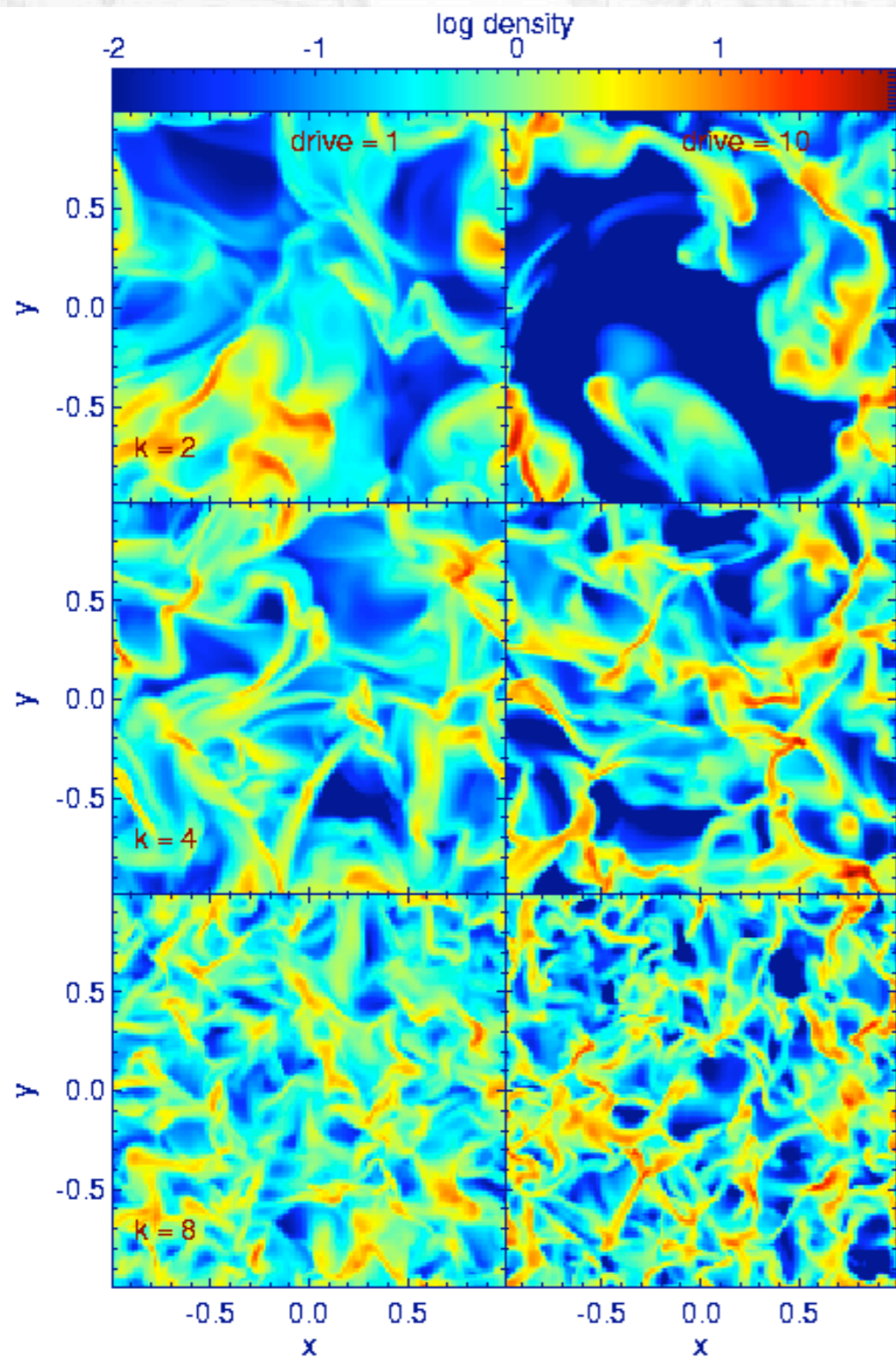
- smoothed particle hydrodynamics (SPH) (Lagrangian method)
- periodic boundaries
- sink particles
- resolving large density contrasts, long timescale



$t = 6.41$



# Numerical Simulations



(Mac Low 1999)

- isothermal equation of state
- two models contracting from initial Gaussian conditions without turbulence
- different turbulent environments:  $0.1 \leq \mathcal{M} \leq 10$ ,  $k = 1..2, 3..4, 7..8$
- initial conditions typical for observed star-forming regions
- magnetic fields, feedback mechanisms neglected

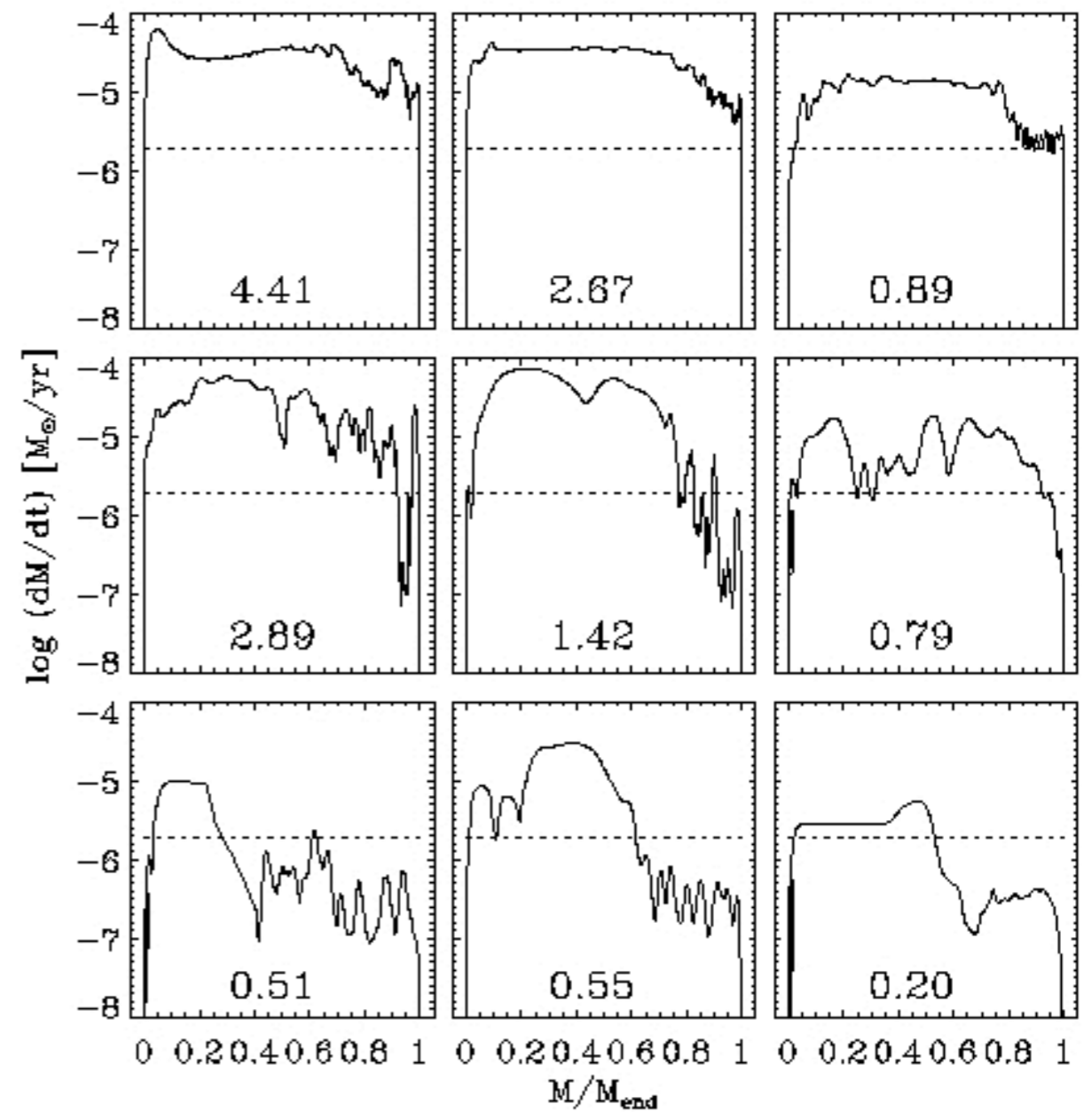
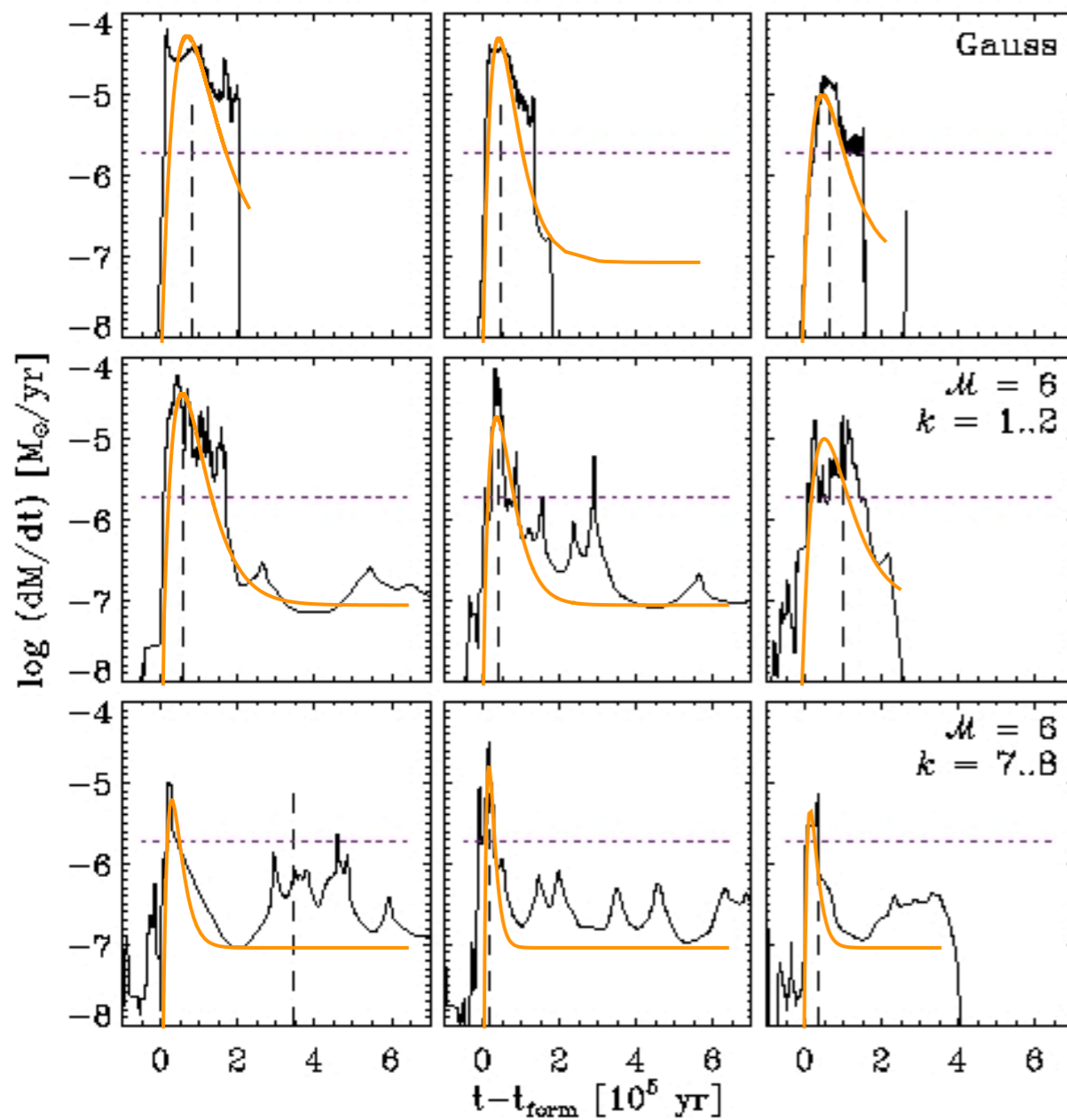
# Properties of Embedded Clusters

- **local properties** (properties of individual objects):
  - properties of individual clumps (e.g. shape, radial profile)
  - accretion history of individual protostars
  - SEDs of individual protostars
  - $T_{\text{bol}}-L_{\text{bol}}$  evolution, evolutionary tracks
- **global properties** (statistical properties):
  - SF efficiency
  - SF time scale
  - initial mass function (IMF)
  - number ratios of YSOs
  - structures of young star clusters

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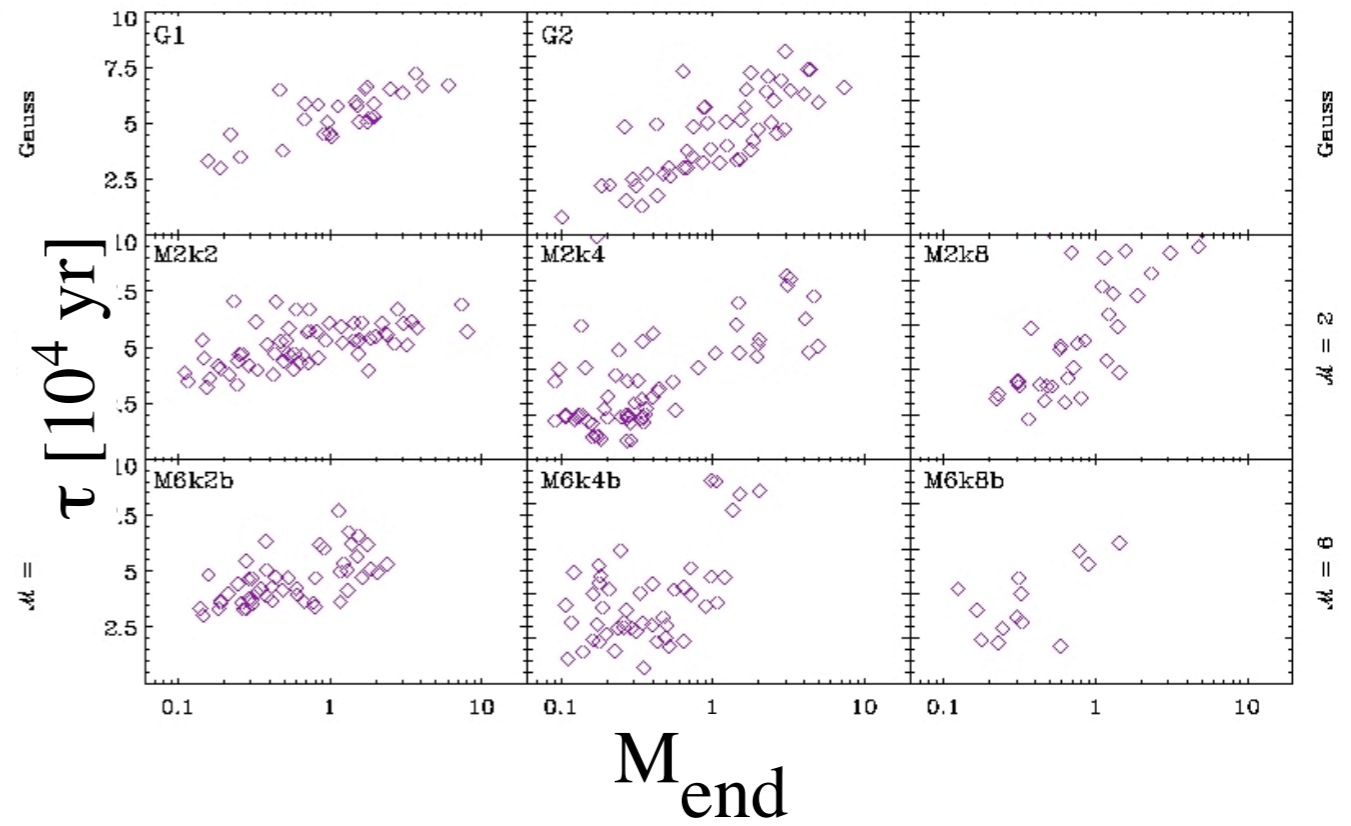
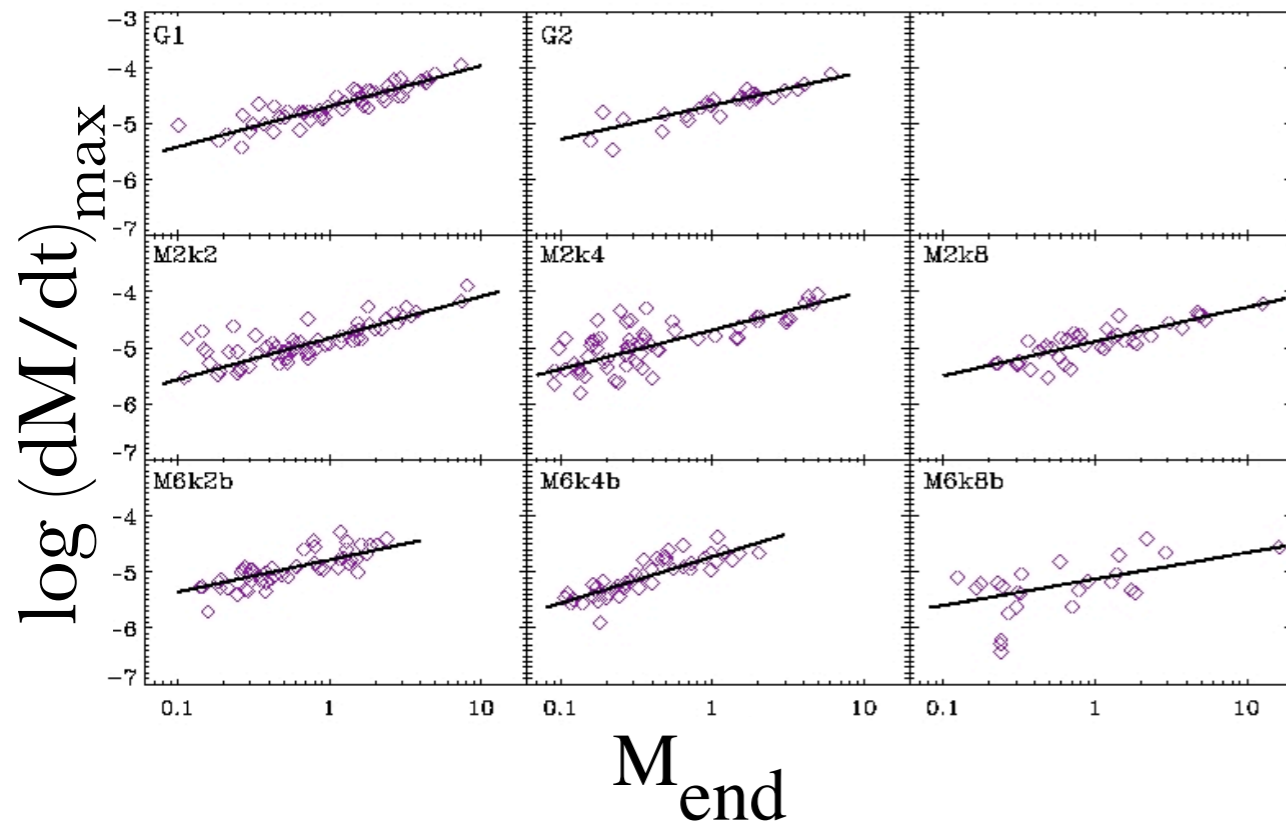
# Mass Accretion History



$$\log \dot{M}(t) = \log \dot{M}_0 - \frac{e}{\tau} t e^{-t/\tau}$$

(Schmeja & Klessen 2004)

# Fit Parameters



log  $\dot{M}_0$ : log  $(dM/dt)_{\max}$

$\tau$ : time of  $(dM/dt)_{\max}$   
related to local free-fall time/local  
density at onset of collapse

# Observations

Mass accretion rates cannot be measured directly from observations → estimated from SEDs or outflow strengths

**Class 0 protostars:**  $\sim 10^{-5} \dots \sim 10^{-4} M_{\text{sun}}/\text{yr}$

**Class I protostars:**  $\sim 10^{-7} \dots \sim 5 \times 10^{-6} M_{\text{sun}}/\text{yr}$

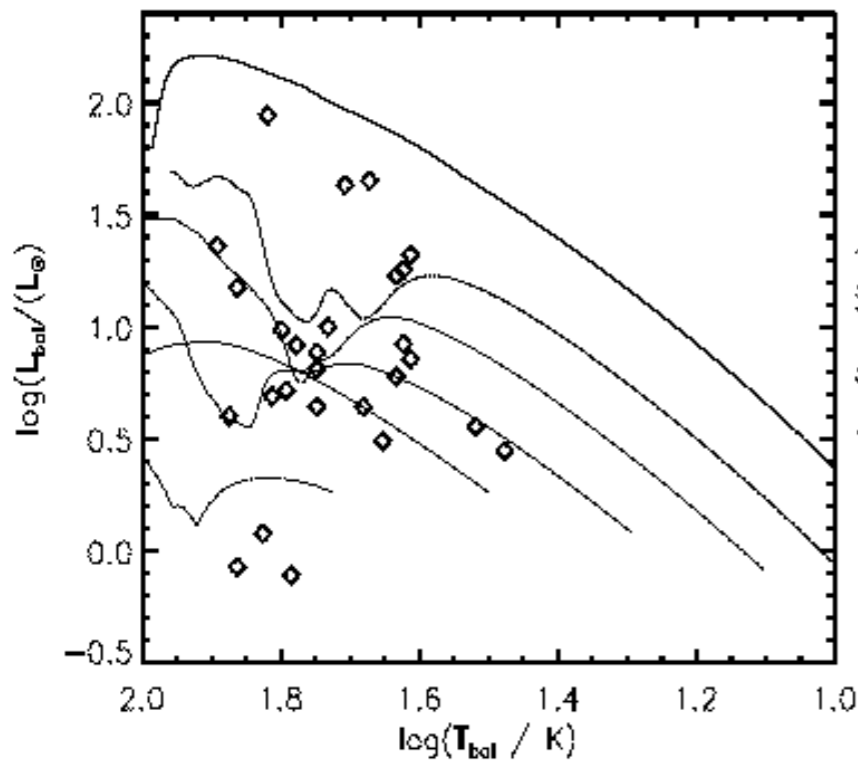
$dM/dt \sim$  one order of magnitude higher in Class 0 phase:  
good agreement with our values

$dM/dt$  hard to observe → conversion of  $dM/dt$  into easier observable quantities like  $T_{\text{bol}}$ ,  $L_{\text{bol}}$

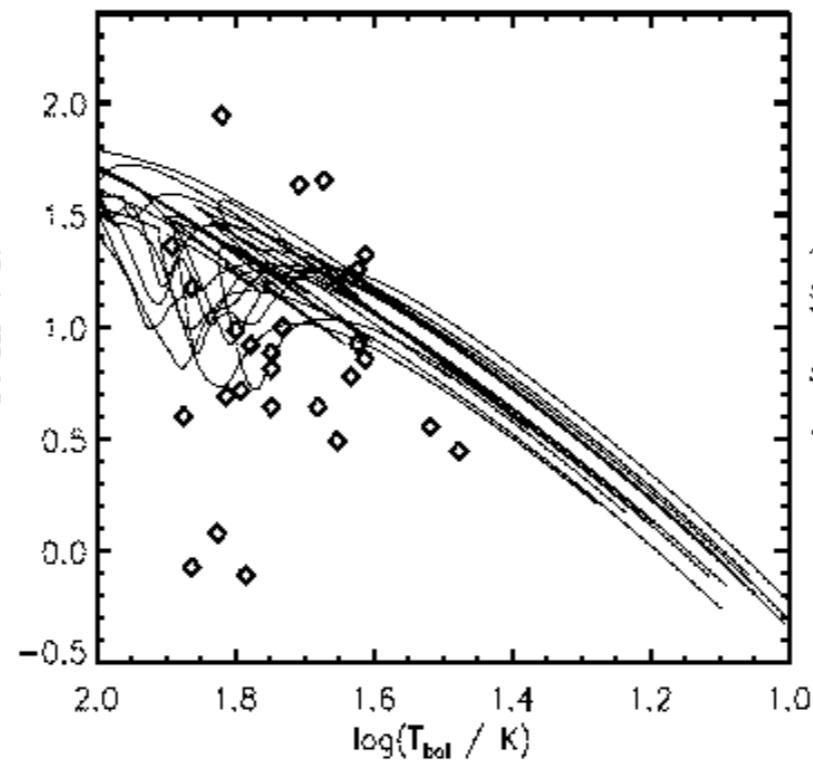
# Evolutionary Tracks

combination of mass accretion rates from gravoturbulent models with evolutionary code (Smith 2000)  $\rightarrow$   $L_{\text{bol}} - T_{\text{bol}}$  diagram

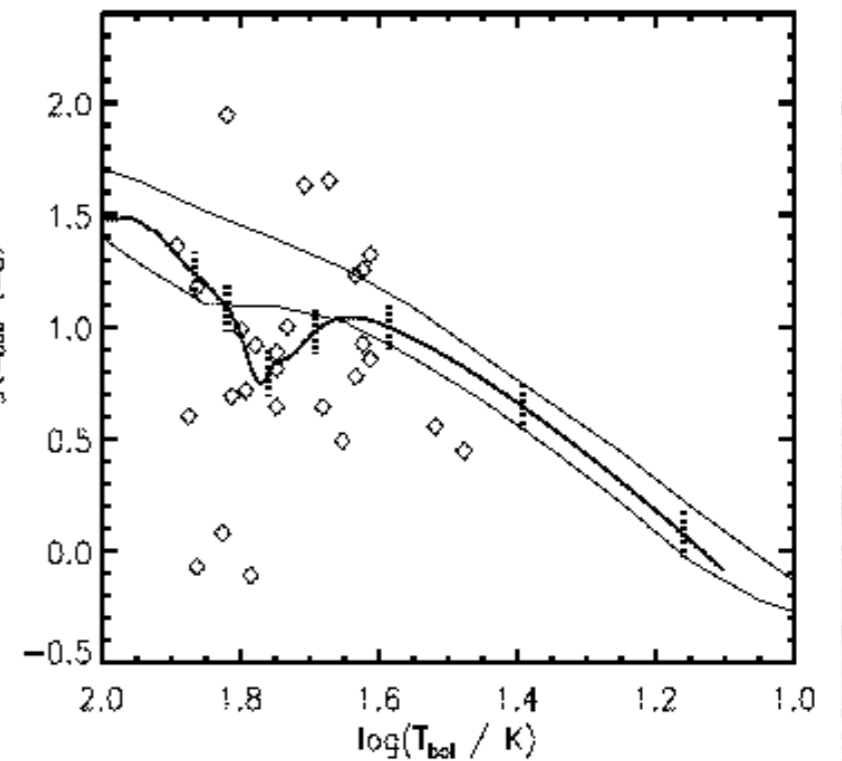
Can we predict final masses, ages...?



tracks for averaged  $dM/dt$   
in six mass bins



all individual tracks in  
mass bin 0.8-1.6  $M_{\text{sun}}$

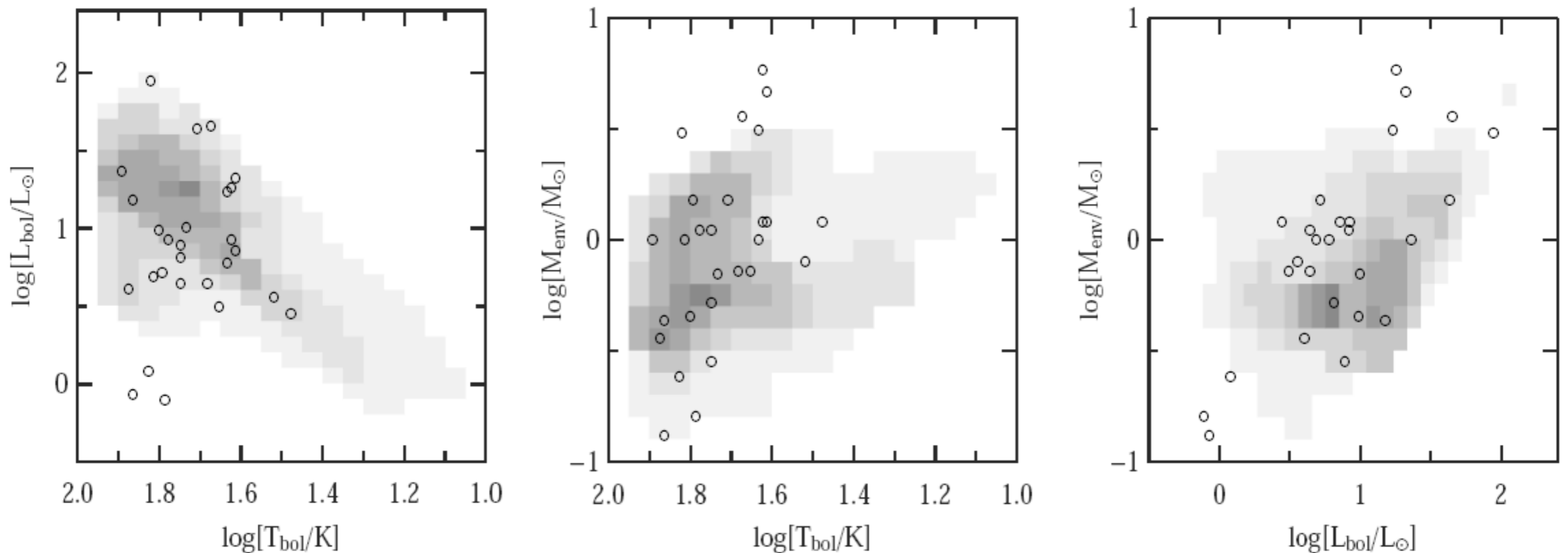


average  $dM/dt$  in mass bin  
0.8-1.6  $M_{\text{sun}}$ ,  $1\sigma$  scatter

(Froeblich, Schmeja, Smith & Klessen 2006)

# Comparison with Observations

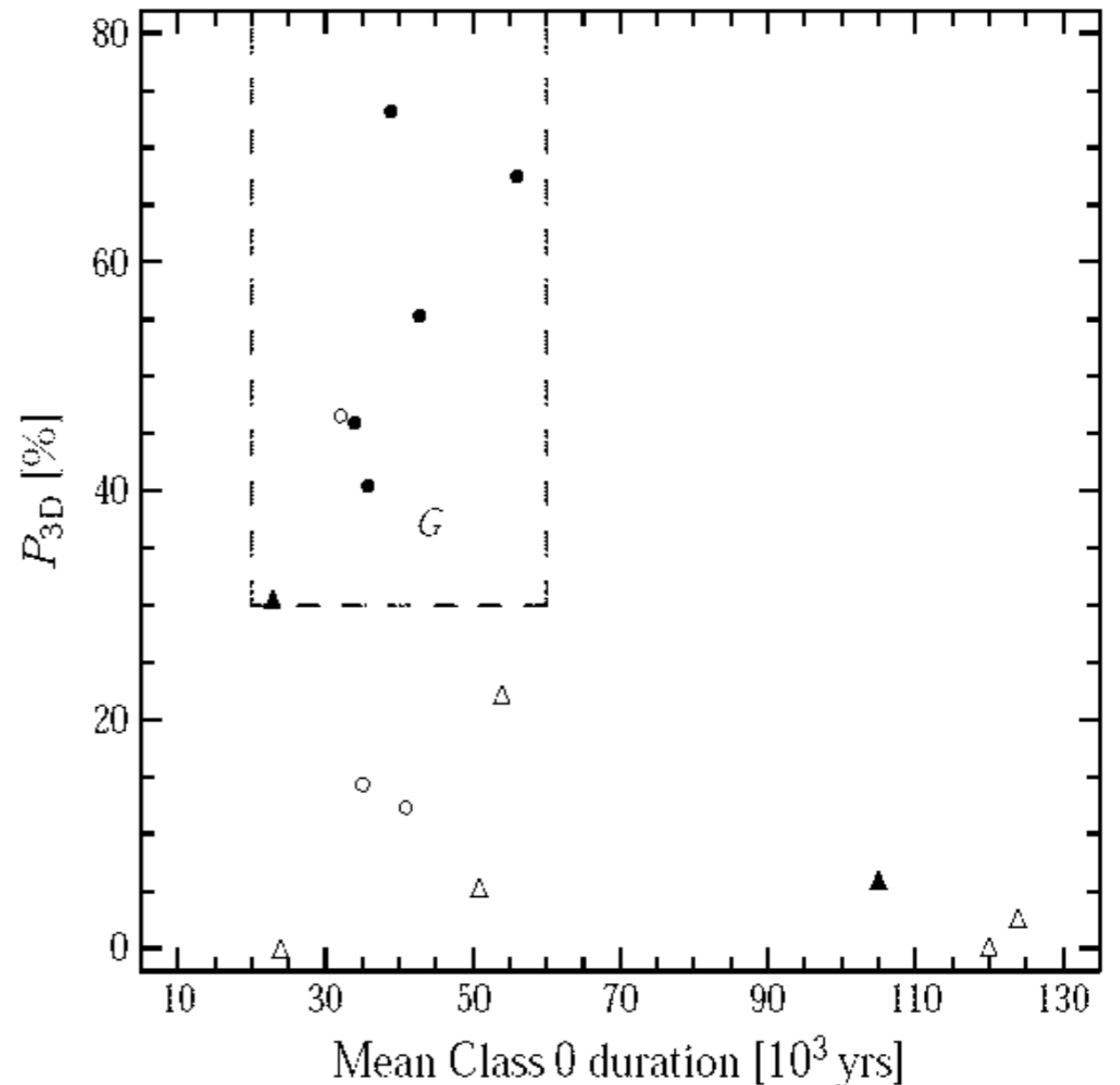
- All tracks of one model  $\rightarrow$  3D probability diagram ( $L_{\text{bol}}$ ,  $T_{\text{bol}}$ ,  $M_{\text{env}}$ ): comparison with sample of observed Class 0 sources ([Froebrich 2005](#)) by 3D Kolmogorov-Smirnov test





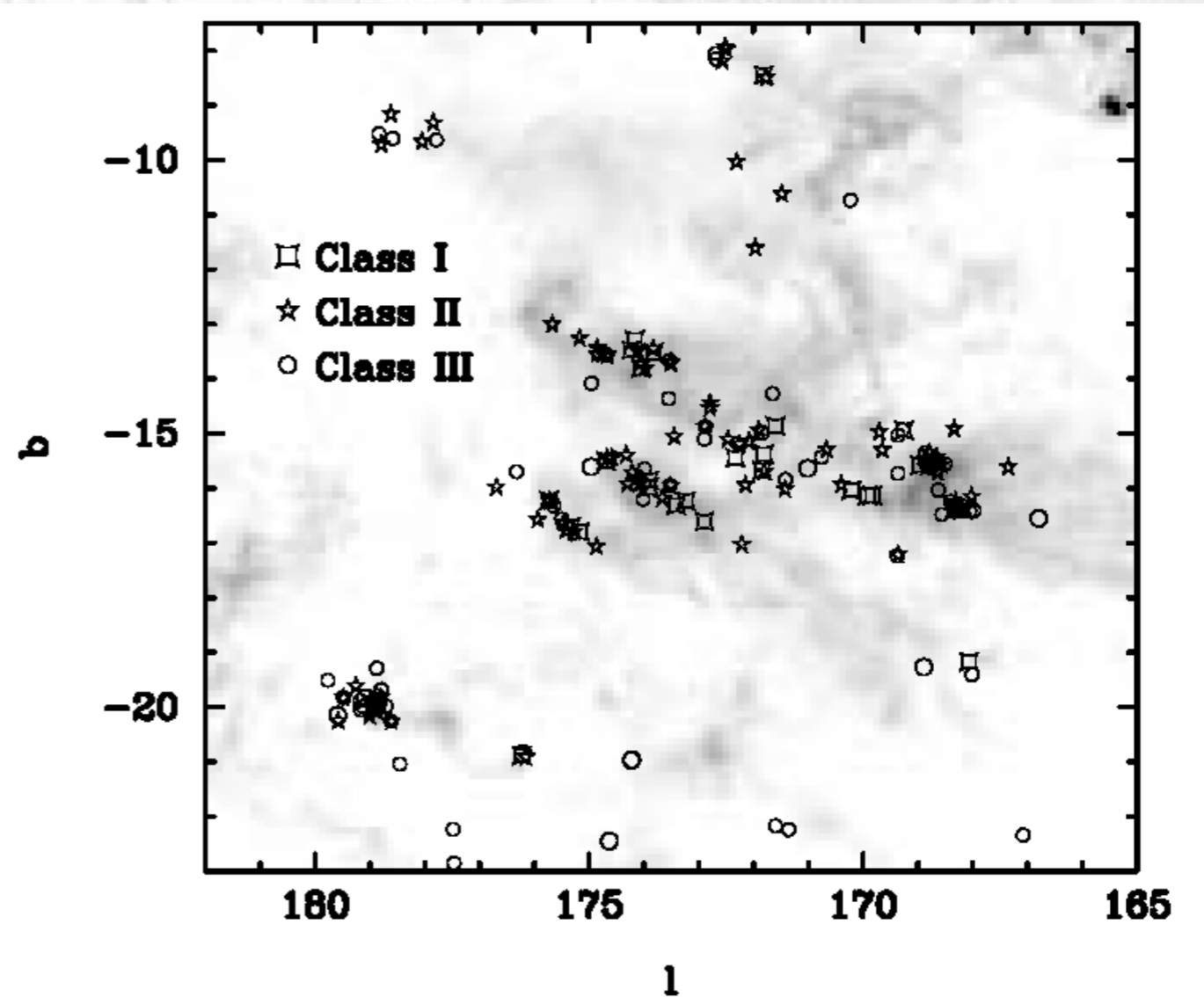
# Comparison with Observations

- max. 70% probability
- best agreement for Class 0 duration of  $2 \dots 6 \times 10^4$  yr
- no correlation with turbulent environment ( $\mathcal{M}$ ,  $k$ )
- all sources in Taurus: underluminous, worse correlation → other mechanism than turbulence?



# Structures of Embedded Clusters

- (almost) all stars form in clusters
- quantitative statistical measure of structure important for understanding the formation and evolution of young star clusters

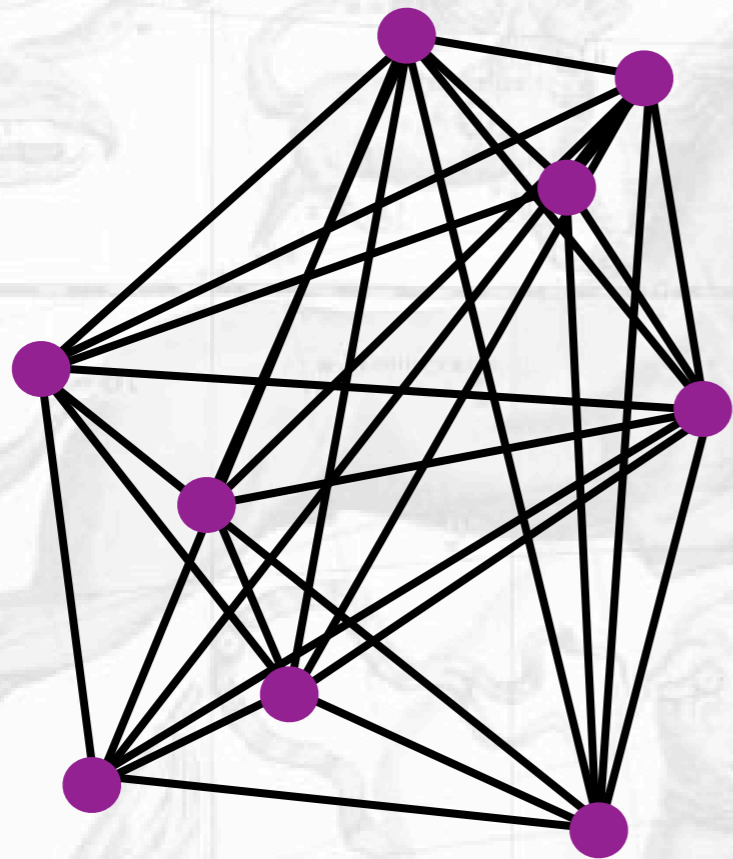


(Hartmann 2002)

# Statistical Methods

- Distribution of source separations
- Mean surface density of companions (Larson 1995):
  - average number of neighbours per square degree on the sky at an angular separation  $\vartheta$
- Normalised correlation length (Cartwright & Whitworth 2004)
- Minimum spanning tree (MST) (Cartwright & Whitworth 2004)

# Normalised Correlation Length

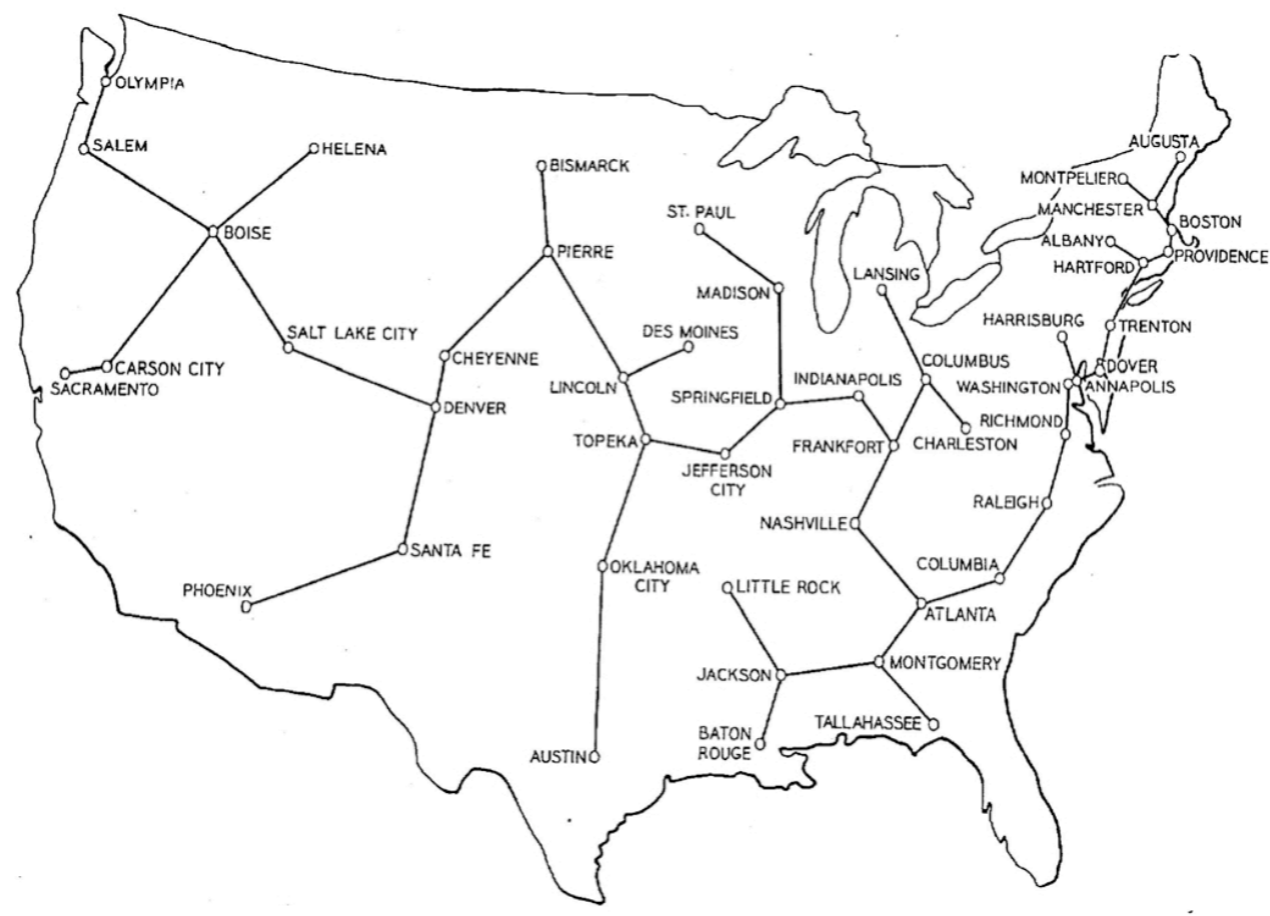


- mean separation between stars in the cluster, normalised by cluster radius
- better indicator for cluster behaviour than MSDC
- independent of the number of stars

→ normalised mean correlation length  $\bar{s}$

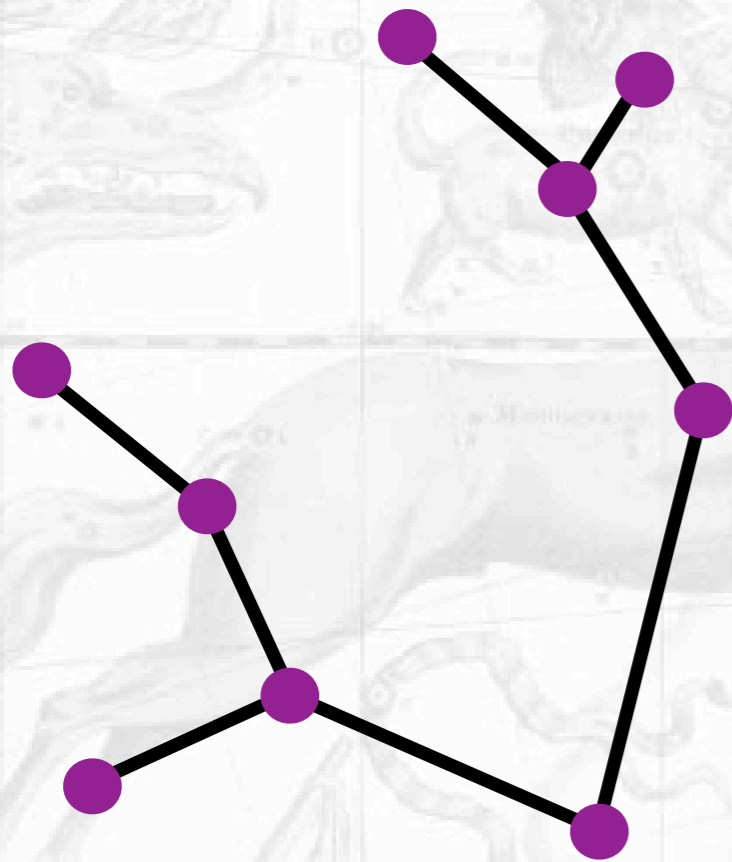
# Minimum Spanning Tree

- construct from graph theory (Kruskal 1956; Prim 1957)
- unique set of edges connecting a given set of points without closed loops, such that the sum of edge lengths is a minimum
- used in many fields (telecommunications, genetics, biology...); astrophysics: structures of galaxy clusters



(Prim 1957)

# Minimum Spanning Tree



MST  $\rightarrow$  mean edge length  $m$

$m$  not independent of number of points  $\rightarrow$  normalised with factor

$\sqrt{A/n}$  (Marcelpoil 1993)

$A$  ... area

$n$  ... number of points

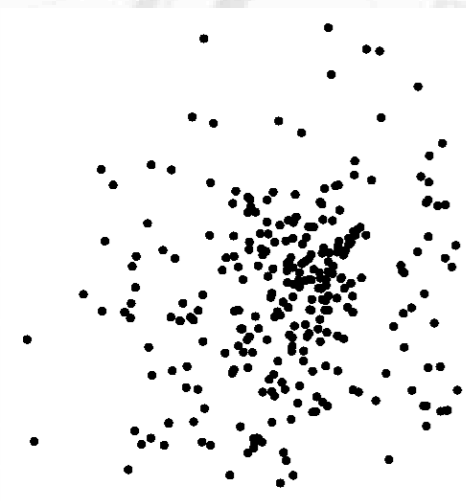
$\rightarrow$  normalised mean edge length  $\bar{m}$

# Q

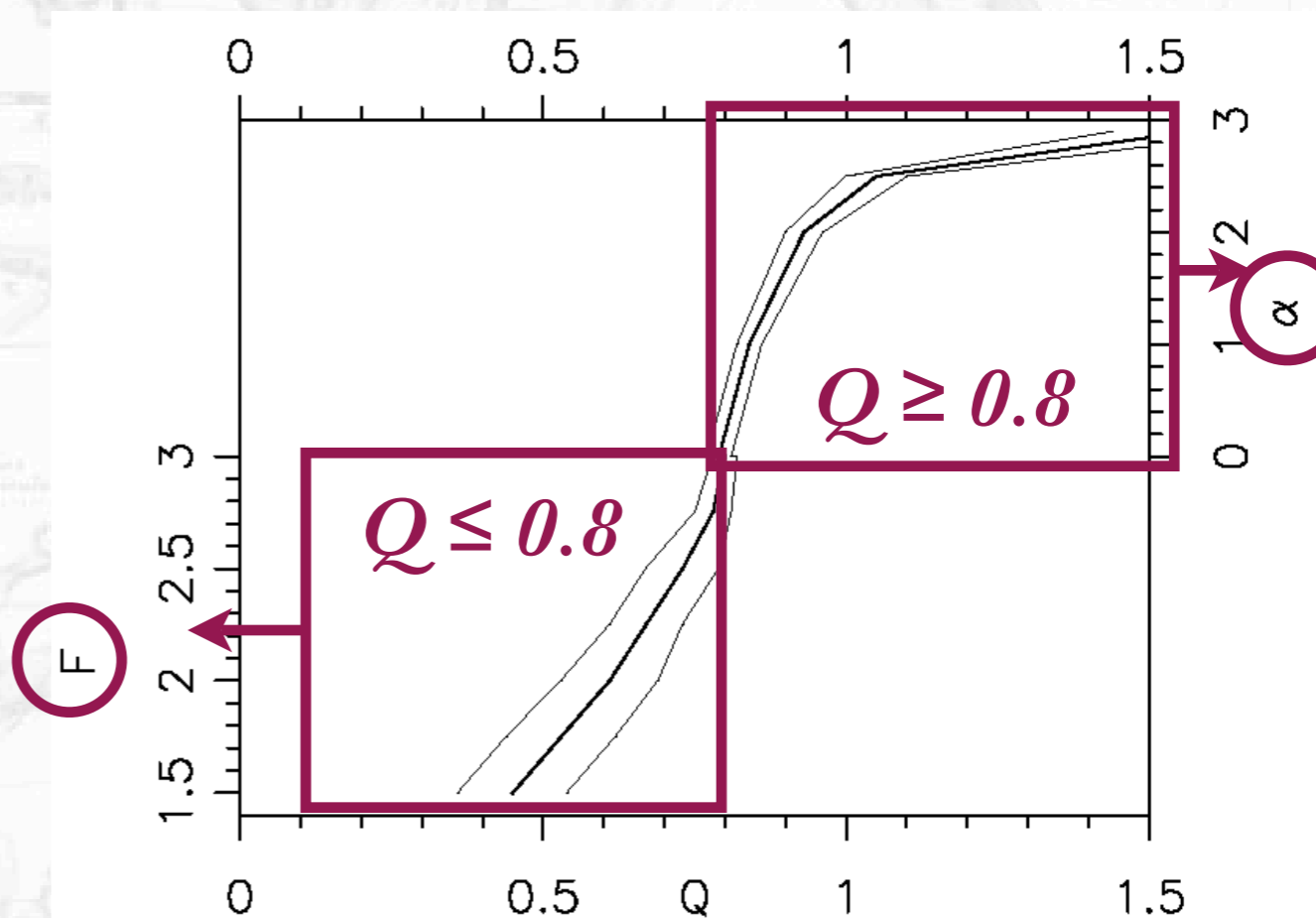
**Q** (Cartwright & Whitworth 2004): distinction between smooth large-scale density gradient and fractal subclustering

$$Q = \frac{\bar{m}}{\bar{s}} = \frac{\text{normalised mean edge length}}{\text{normalised correlation length}}$$

**$Q \geq 0.8$ :**  
centrally concentrated clusters with volume density  
 $n \propto r^{-\alpha}$



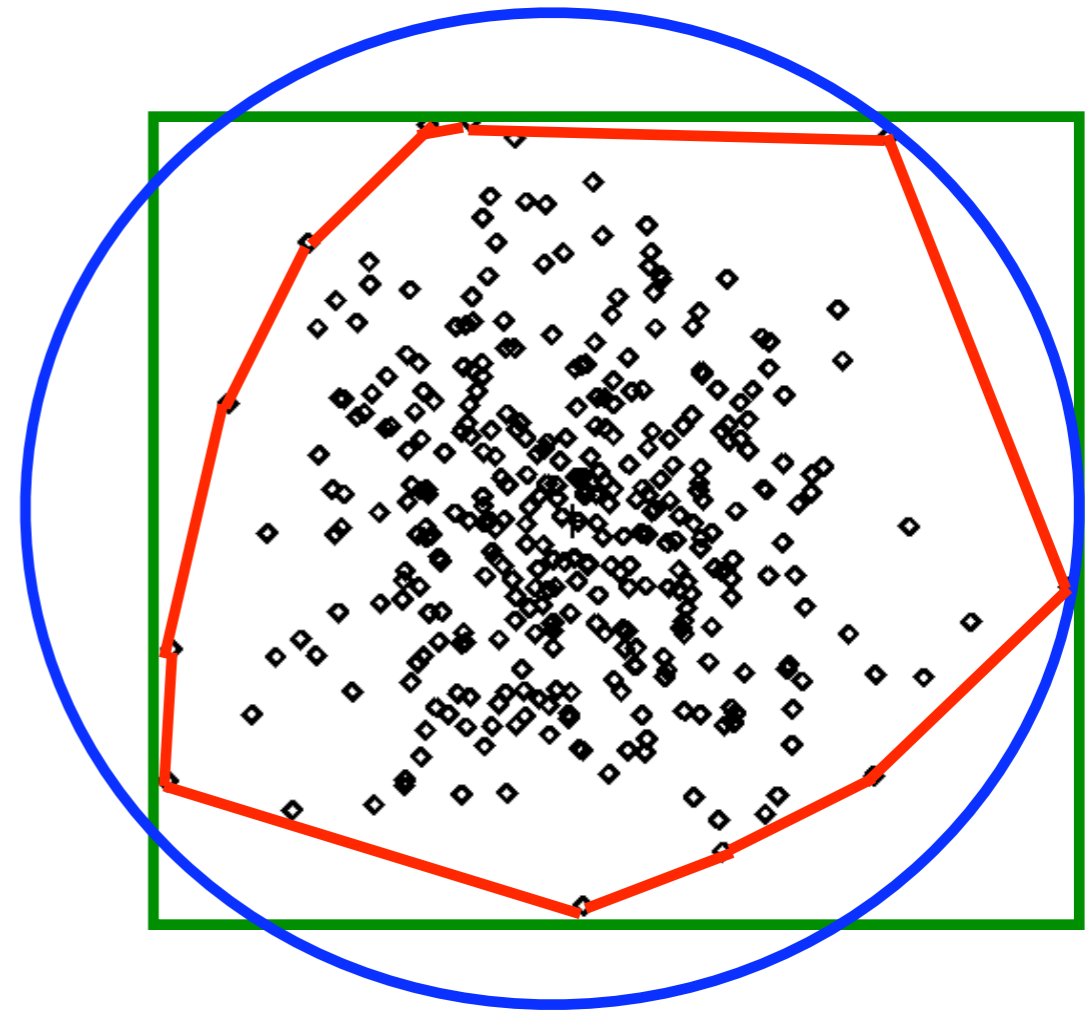
**$Q \leq 0.8$ :**  
clusters with fractal substructure, fractal dimension  $F$



(Cartwright & Whitworth 2004)

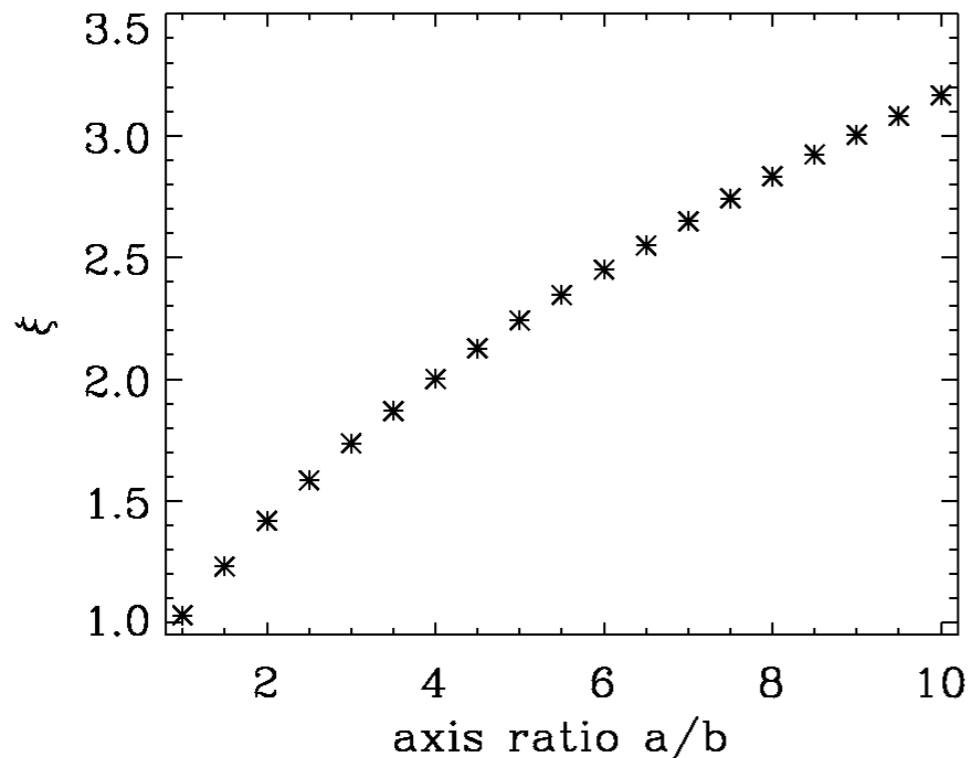
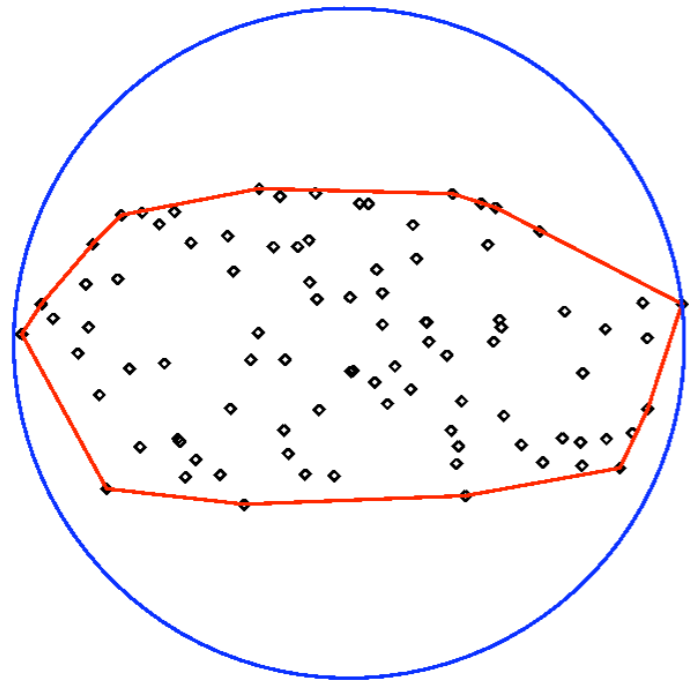
# Area of a Cluster

- $m$ ,  $s$  normalised by cluster radius/area
- How to define the cluster area?
- different approaches: circle, rectangle, convex hull
- definition crucial, can differ by factor of 2 or more
- $Q = \bar{m}/\bar{s}$  independent of radius/area!





# Elongation of a Cluster



- elongation  $\xi$  of a cluster:

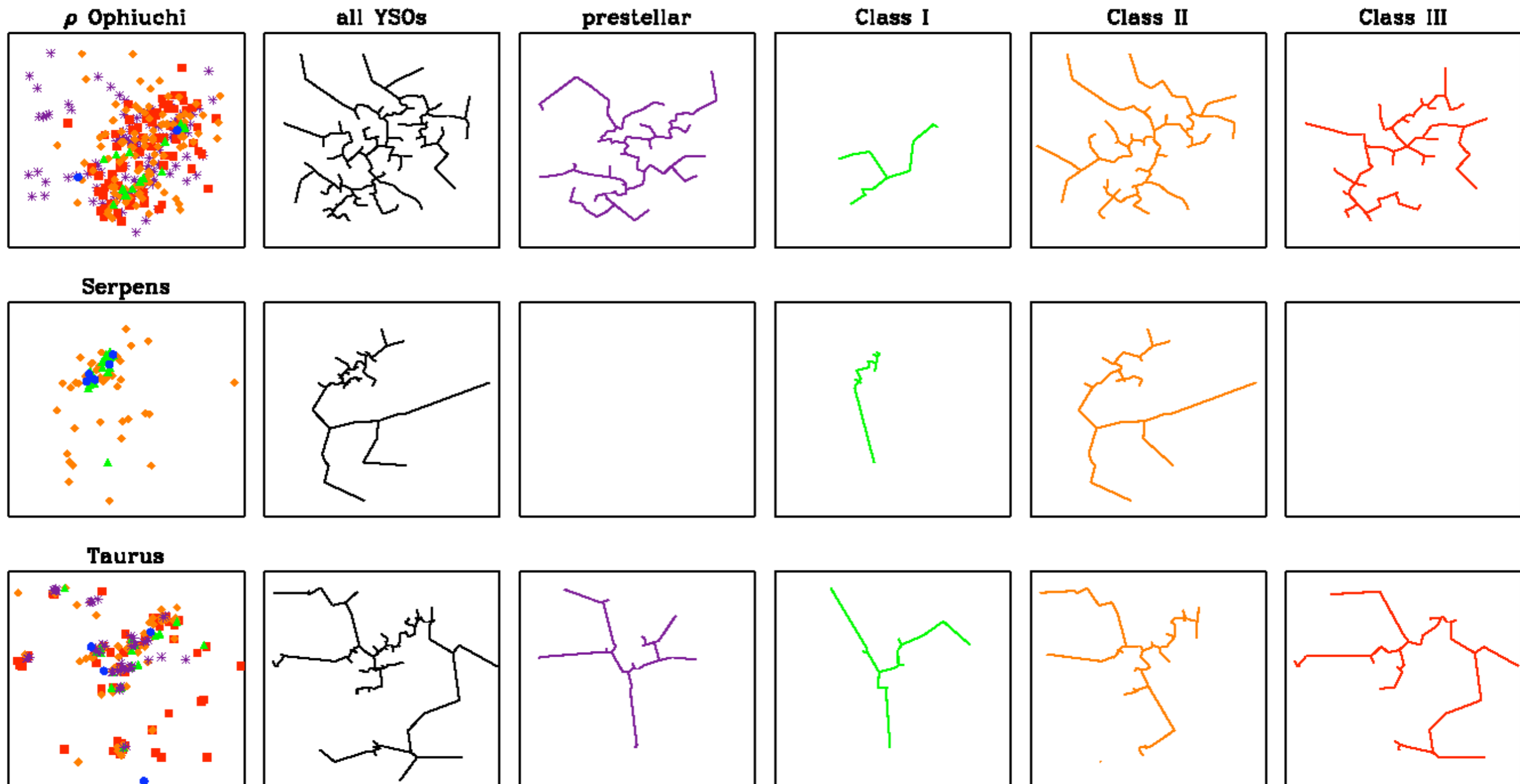
- $$\xi = \frac{R_{\text{cluster}}^{\text{circle}}}{R_{\text{cluster}}^{\text{conv.hull}}}$$

- $\xi \approx 1$ : spherical cluster,
- $\xi \approx 3$ : elongated elliptical cluster with axis ratio of  $a/b \approx 10$

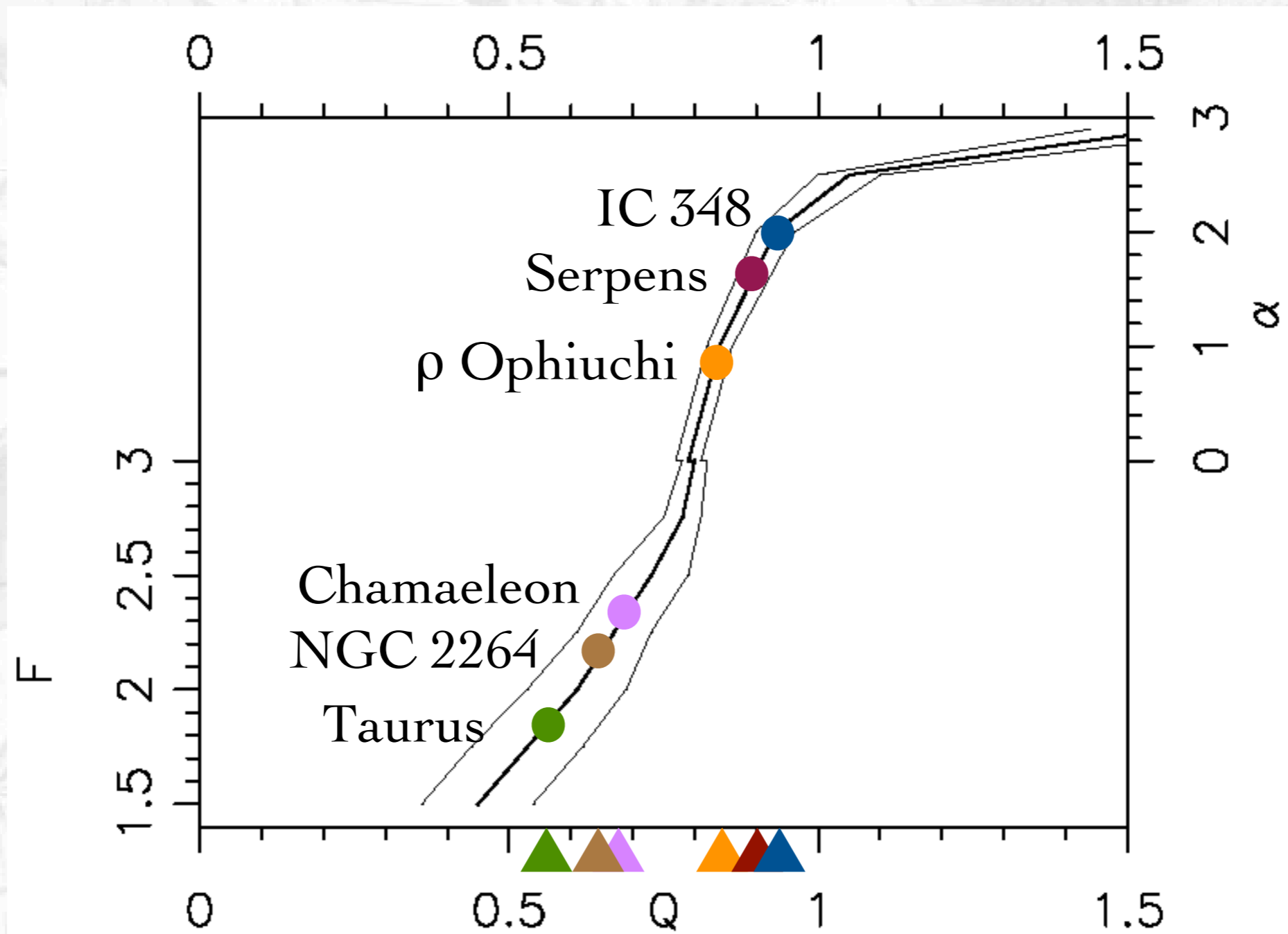
# Observations

- data: sample of YSOs and prestellar cores constructed from various published sources ([Schmeja et al. 2005](#))
- **$\rho$  Ophiuchi, Serpens, Taurus:** all classes
- **Chamaeleon I, IC 348:** no information on individual classes
- **Caveat:** different samples  $\rightarrow$  different completeness limits
- **Caveat:** 2D projections, not 3D structure!

# Observations: MST



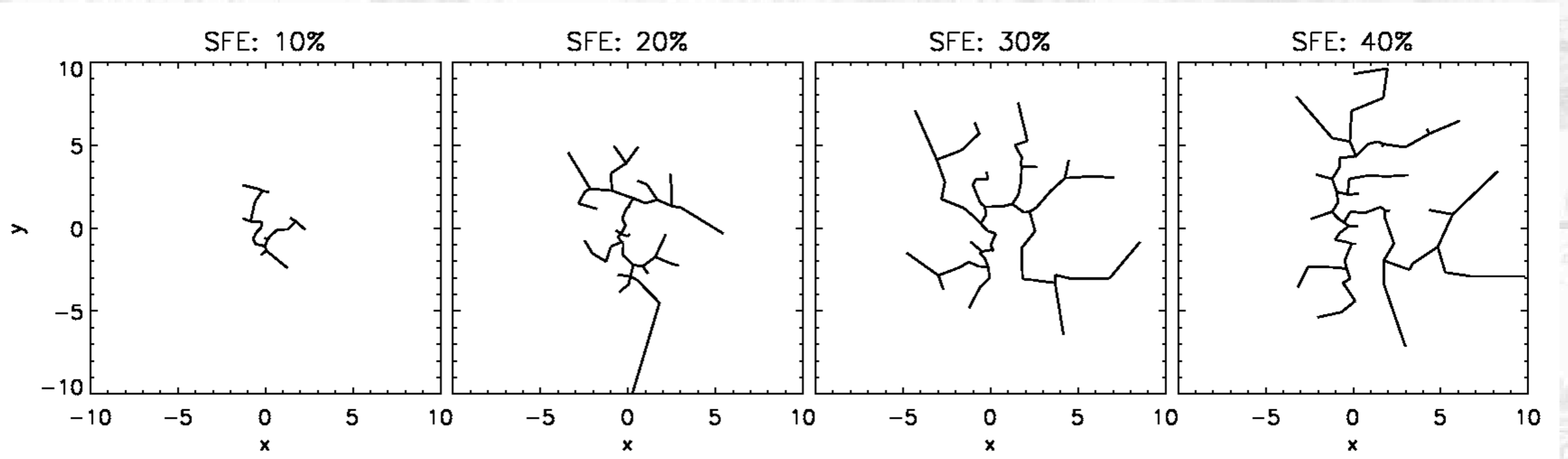
# Observations: $Q$



(Cartwright & Whitworth 2004)

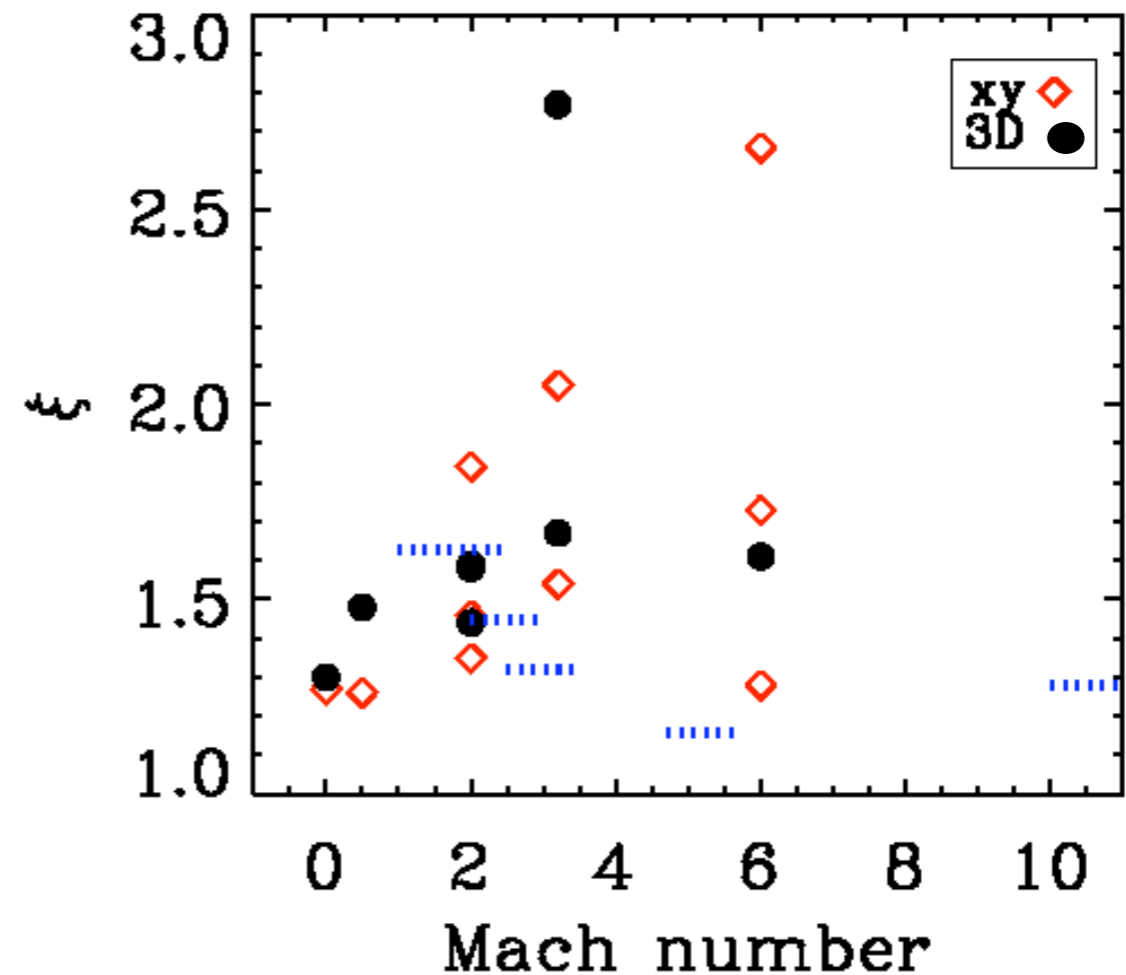
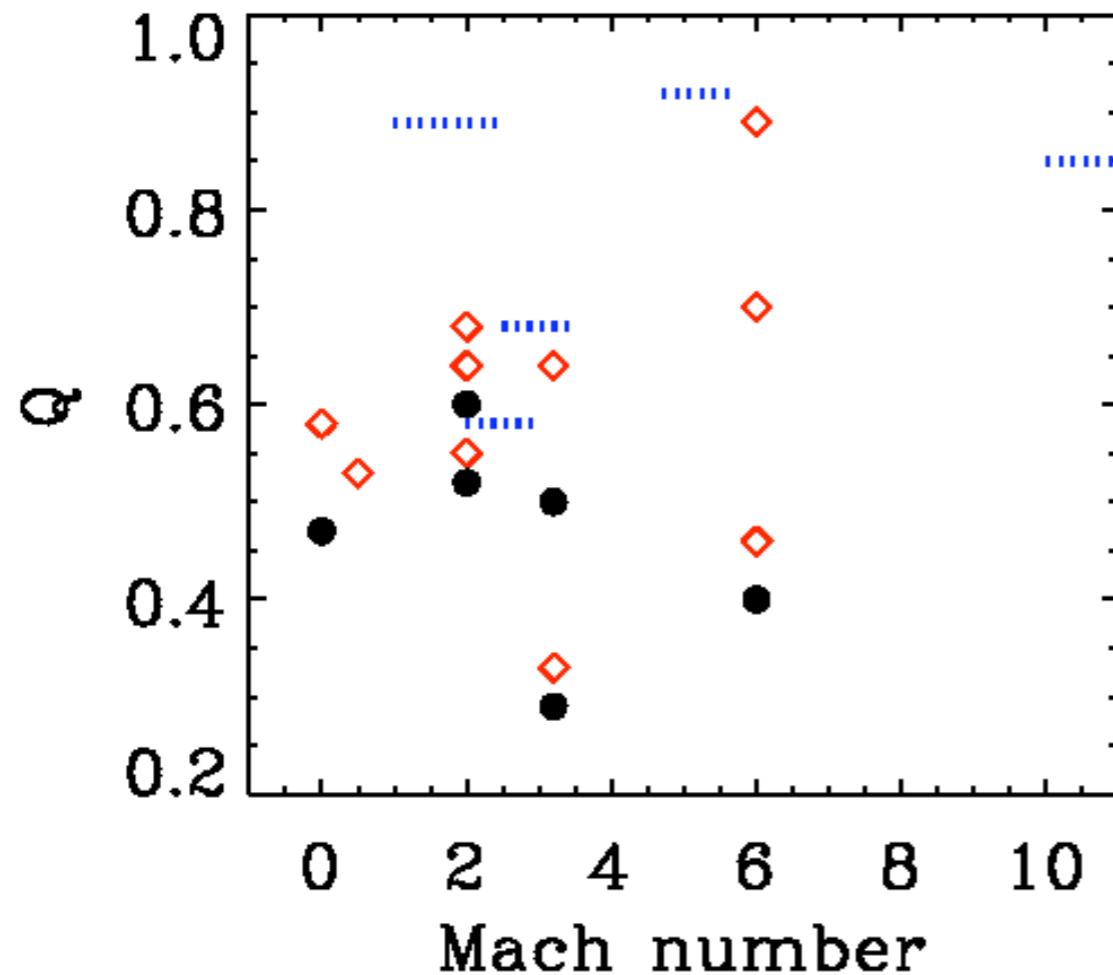
# Models: MST

Models: 3D, projection into 2D planes



MST of one model ( $\mathcal{M} = 6, k = 3..4$ ) projected into the xy-plane at different times (SFEs): expansion of the cluster

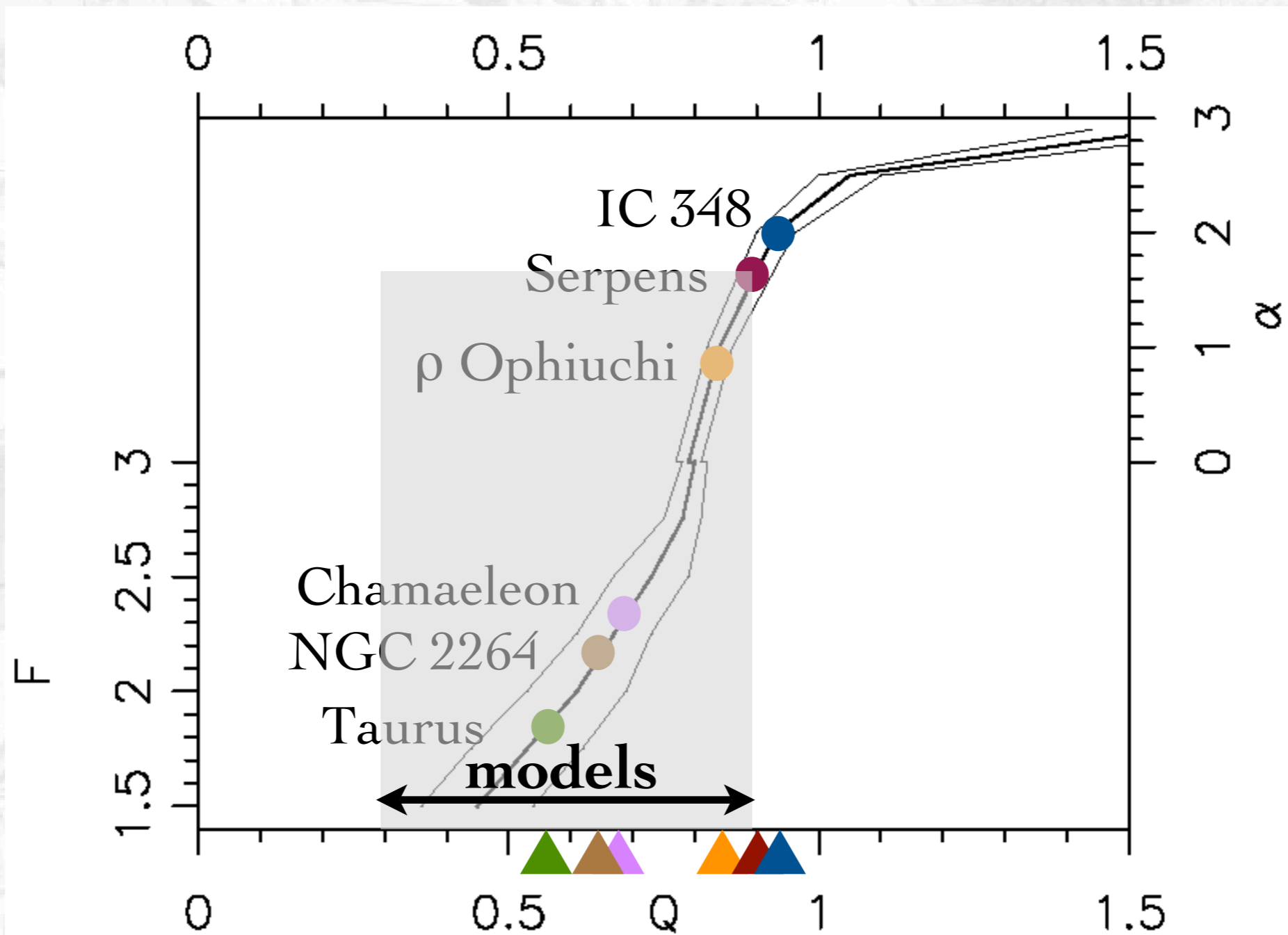
# Models: Parameters



..... Serpens - Taurus - Cha I - IC 348 -  $\rho$  Oph

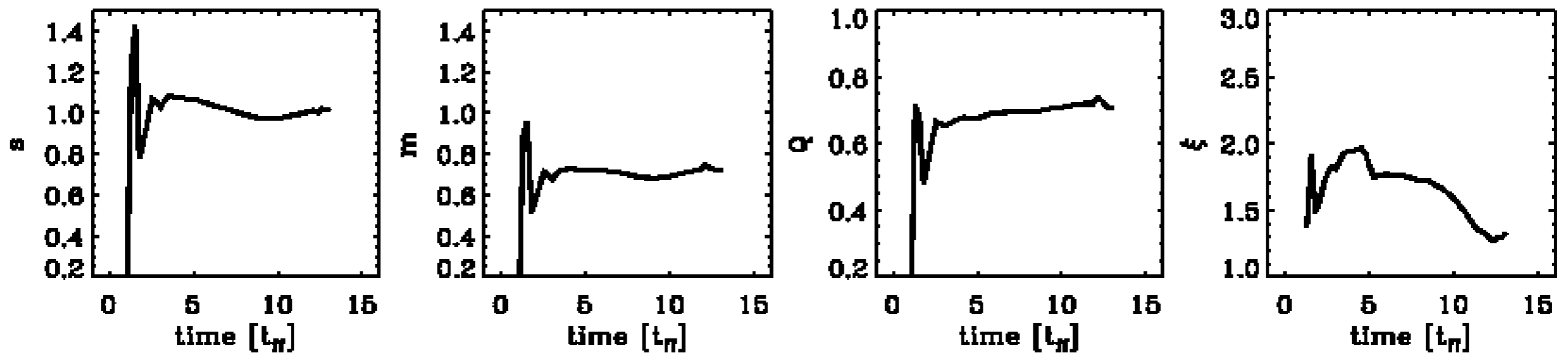
- no correlation with  $\mathcal{M}$  or  $k$
- good agreement between models and observations when similar  $\xi$  values

# Models: $Q$



(Cartwright & Whitworth 2004)

# Models: Temporal Evolution

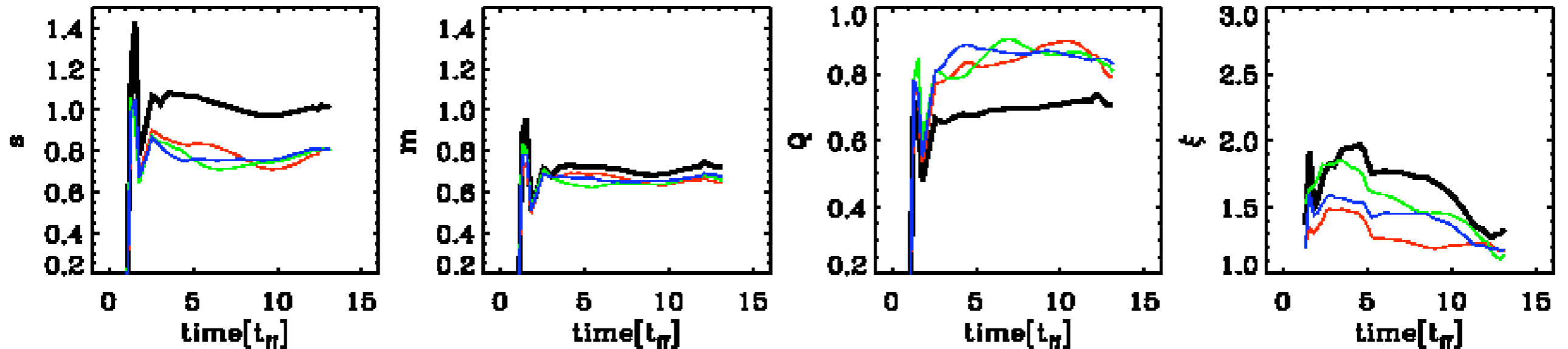


- similar behaviour of all models
- $\bar{s}$ ,  $\bar{m}$  decline slightly,  $Q$  increases
- star formation sets in in different regions, cluster becomes more centrally concentrated as more and more gas is turned into stars



# Models: Effect of Projection

models: 3D distribution projected into xy-, xz-, yz-plane

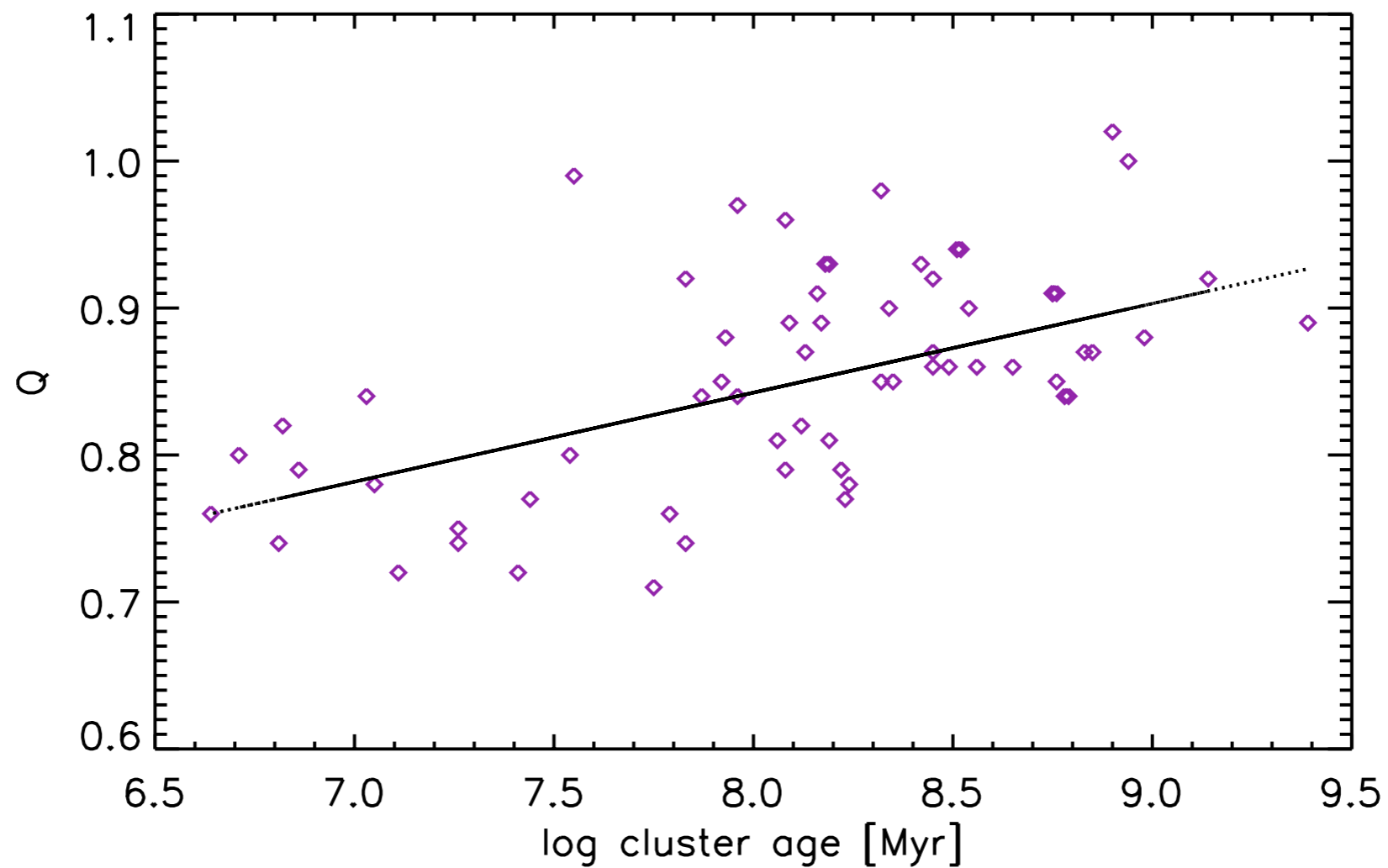


$$\bar{s}_{3D} / \bar{s}_{2D} \approx 1.2, \bar{m}_{3D} / \bar{m}_{2D} \approx 1.1$$

individual values can change, but qualitative behaviour of evolution similar

# Evolution: Open Clusters

sample of 63 open clusters (Kharchenko et al. 2004, 2005):



correlation of  $Q$  with cluster age?

# Summary

- gravoturbulent models of SF predict many observed properties
- mass accretion rates highly time-dependent
- no unique protostellar evolutionary tracks
- Class 0 duration:  $2 \dots 6 \times 10^4$  yr
- protostars in Taurus: anomalous accretion history → other control mechanism?
- not all prestellar cores may form stars
- clusters build up from several subclusters, evolve to more centrally concentrated state